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12

ON PARACHUTIST DYNAMICS

Ronald L. Huston

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Cincinnati, Ohio 45221

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Technical Report for Office of Naval Research  
under Contract N00014-76C-C139

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# ABSTRACT

The dynamics of a parachutist is discussed. Results of a computer simulation and a parameter study are presented. A variety of initial parachutist configurations prior to "opening shock" are considered and the relative effects upon the parachutist's dynamics -- particularly, the head/neck system dynamics -- are studied. Optimal initial (pre-opening) configurations which minimize the subsequent force and moment pulses experienced by the head/neck system, are identified and discussed. Application in parachute design and in developing jumping strategies are also discussed.

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## NOTATION

- $a_{ik}$  - Governing differential equation coefficients (See Equation (5).)
- $\underline{a}_j$  - Acceleration of  $G_j$  in a Newtonian reference frame
- $A_j$  - Projected profile area of body  $B_j$
- $B_j$  - A typical body of the system
- $C_D$  - Drag coefficient
- $\underline{D}_j$  - Resultant air drag force on body  $B_j$  (See Equation (1).)
- $\underline{f}_1$  - Generalized force array (See Equation (5).)
- $\underline{F}_j$  - Inertia force on  $B_j$  (See Equation (3).)
- $G_j$  - Mass center of body  $B_j$
- $L$  - Point of application of the left riser force (See Figure 1.)
- $m_j$  - Mass of  $B_j$
- $\underline{n}_j$  - A unit vector parallel to the axis of  $B_j$
- $R$  - Point of application of the right riser force (See Figure 2.)
- $\underline{V}_j$  - Velocity of  $G_j$  relative to the air and perpendicular to the axis of body  $B_j$  (See Equation (2).)
- $\underline{V}_W$  - Ambient air velocity
- $X_j, Y_j, Z_j$  - Coordinate axes of body  $B_j$
- $\underline{\alpha}_j$  - Angular acceleration of  $B_j$  in a Newtonian reference frame
- $\rho$  - Mass density of air
- $\psi_k$  - Generalized coordinates
- $\underline{\omega}_j$  - Angular velocity of  $B_j$  in a Newtonian reference frame

## INTRODUCTION

This report presents the results of a computer-aided parameter study on parachutist dynamics. Particular attention is given to head/neck dynamics. The objective of the parameter study is to obtain optimal initial configurations, prior to opening shock, which will minimize the forces and moments experienced by the head/neck system.

During the past decade, there has been an increasing interest in parachutist dynamics during and immediately after the opening of the parachute. This interest stems from the high incidence of injuries occurring in emergency egress from high speed aircraft. Since most of the permanent disabilities are the result of injuries to the head/neck system, the major concern of researchers has been the parachutist's head/neck dynamics. These interests and concerns have stimulated the development of a number of experimental studies of parachutist response. These studies have used both volunteers and dummies in a variety of jumping configurations. A summary of some of these experiments are contained in papers by Palmer, Call, and Ewing [1,2]\*. Also, studies on opening shock and parachute opening theory have been conducted by Heinrich and Saari [3]. Performance data for various types of parachute assemblies and harnesses has been tabulated by Woolman [4].

In a recent paper, Huston, Winget, and Harlow [5] suggested that it may be possible to obtain analytical simulation of parachutist dynamics

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\*Numbers in brackets refer to references at the end of the report.

by using a biodynamic computer model of the parachutist. Indeed, by using a modified version of the UCIN Crash Victim computer model [6-10], they were able to exhibit a reasonably close correspondence between analytical and experimental data. These encouraging results were a motivating factor for the parameter study summarized in this report.

The report itself is divided into three parts with the following part providing a description of the biodynamic model and the forces applied to it. This is followed by a description of the governing dynamical equations. The final part provides a summary of the results as well as conclusions regarding optimal initial configurations.

## THE BIODYNAMIC PARACHUTIST MODEL

Figure 1. contains a schematic representation of the model. It consists of a system of connected rigid bodies simulating the human frame. The arms and legs are represented by frustrums of elliptical cones. The torso and neck are elliptical cylinders and the head is a spheroid. The bodies are connected by spherical joints. Nonlinear springs and dampers are used between adjacent bodies to simulate the ligaments and muscles and to limit the range of motion [7,10,11].

The model has 13 bodies and thus it has 42 degrees of freedom (3 rotational degrees of freedom for each body and a translational degree of freedom for a reference body, say  $B_1$ ). This model is a modification of the model used in Reference [5]. The difference is the inclusion of a neck segment, thus improving the accuracy of the modelling.

The model allows for the arbitrary specification of external forces and moments on each of its bodies. For a parachutist, the externally-applied forces are gravity forces, the riser forces, and the wind or air drag forces. The gravity forces may be represented as vertical (downward) forces passing through the respective mass centers of the bodies. The riser forces are assumed to be applied at the shoulders at points L (left riser) and R (right riser) as shown in Figure 1. The direction of the riser forces is assumed to be opposite to the direction of the velocities of L and R relative to the air. Finally, the air drag forces are represented on each body by a single force passing through the mass center of the body and directed



opposite to the direction of the velocity of the mass center relative to the air. Specifically, if  $B_j$  is a typical body of the system as shown in Figure 2., then the air drag force  $D_j$  on  $B_j$  is given by:

$$\underline{D}_j = -\rho C_D A_j |\underline{V}_j| \underline{V}_j \quad (1)$$

where  $j=1, \dots, 13$ , and where  $\rho$  is the mass density of the air,  $C_D$  is the drag coefficient (dependent upon the Reynolds number),  $A_j$  is the projected profile area of  $B_j$ , and  $\underline{V}_j$  is the component of the velocity of  $B_j$  relative to the air and perpendicular to the axis of  $B_j$ . If  $\underline{V}_W$  is the ambient air velocity,  $\underline{V}_j$  is given by:

$$\underline{V}_j = \underline{n}_j \times [(\underline{V}_j - \underline{V}_W) \times \underline{n}_j] \quad (2)$$

where  $\underline{n}_j$  is a unit vector parallel to the axis of  $B_j$  as shown in Figure 2.

The inertia forces acting on the bodies of the model due to their motion in a Newtonian reference frame may be represented on each body  $B_j$  by a single force  $\underline{F}_j$  passing through  $G_j$ , the mass center of  $B_j$  together with a couple with torque  $\underline{T}_j$ .  $\underline{F}_j$  and  $\underline{T}_j$  may be expressed as [12]:

$$\underline{F}_j = -m_j \underline{a}_j \quad (3)$$

and

$$\underline{T}_j = -\underline{I}_j \cdot \underline{\alpha}_j - \underline{\omega}_j \times (\underline{I}_j \underline{\omega}_j) \quad (4)$$

where  $j=1, \dots, 13$ . and where  $m_j$  is the mass of  $B_j$ ,  $I_j$  is the inertia dyadic of  $B_j$  relative to  $G_j$ ,  $a_j$  is the acceleration of  $G_j$ ,  $\omega_j$  is the angular velocity of  $B_j$ , and  $\alpha_j$  is the angular acceleration of  $B_j$  -- all measured relative to a Newtonian reference frame.

Finally, each body  $B_j$  of the system has a coordinate axes system  $X_j, Y_j, Z_j$  ( $j=1, \dots, 13$ ) where  $X_j$  is forward,  $Y_j$  is to the left, and  $Z_j$  is upward. In a reference configuration of the model, as in Figure 1, the respective coordinate axes are parallel.

## GOVERNING EQUATIONS

When the model is subjected to the forces outlined above, the governing dynamical equations of motion may be conveniently obtained by using Lagrange's form of d'Alembert's principle as developed by Kane et.al. [12-14]. This principle, a virtual work type principle, leads to governing equations whose coefficients are readily converted into algorithms for numerical generation on a computer. Such algorithms have been written resulting in several computer codes called UCIN[5-10,15,16]. In one of these codes, called "PARACHUTE," the governing differential equations take the form:

$$\sum_{k=1}^{42} a_{1k} \ddot{\psi}_k = f_1 \quad (i=1, \dots, 42) \quad (5)$$

where the  $\psi_k$  ( $k=1, \dots, 42$ ) are generalized coordinates corresponding to the degrees of freedom of the system and  $a_{1k}$  and  $f_1$  are generalized inertia and force arrays. The system of Equations (5) is a coupled system of non-linear stiff ordinary differential equations. The system may be integrated numerically using a differential equation solver routine. In the current parameter study, a fourth order Runge-Kutta technique called RKGS was used to numerically integrate the equations.

## RESULTS AND CONCLUSIONS

The parachutist model and its accompanying computer code described above were used in making a parameter study of a parachutist in a variety of initial configurations, prior to opening shock, for a typical low-speed jump, without ambient wind. The riser force data for the study were obtained from experimental data from volunteer jumps at the Naval Air Recovery Facility at El Centro, CA. The physical data for the parachutist model were also obtained experimentally. In the current study, it approximated that of a 75th percentile man.

The study was conducted for 3 inclinations of the spine or torso relative to the vertical and for three initial head and neck inclinations providing a total of 9 different jumping configurations. Specifically, the torso was inclined to the vertical at  $22.5^\circ$ ,  $45^\circ$ , and  $67.5^\circ$ . The initial angle between the head and the neck and between the neck and the upper torso were equal to each other; they have the values  $-15^\circ$ ,  $0^\circ$ , and  $15^\circ$ . The initial configurations of the arms and legs were "spread-eagle" and were the same for all computer runs.

The X, Y, and Z components of the riser forces relative to a Newtonian reference frame varied only slightly with the initial configuration. Typical values are shown graphically in Figures 3., 4., and 5. Using such riser forces together with the physical parameters and the initial conditions, the coefficients of the governing differential equations were computed and the equations were numerically integrated. The results of this integration were time histories of the generalized coordinates and

their derivatives. These, in turn, were used to determine the head and neck motion and the internal restraining forces and moments on the head/neck system. Figures 6. to 17. show the resulting head rotation relative to the neck and the neck rotation relative to the upper torso for the various combinations of the initial head, neck, and torso inclination angles. The "alpha" rotation corresponds to "roll" about the X-axis and the "beta" rotation corresponds to "pitch" about the Y-axis. Figures 18. to 29. show the components and magnitude of the resultant restoring force between the head and neck for the various initial head, neck, and torso inclination angles. Figures 30. to 38. show the X and Y components and magnitude of the restraining moment between the head and neck for the various initial configurations. (The Z components of the moments were negligible.) Finally, Figures 39., 40., and 41. show the Y component of the angular acceleration of the head relative to the upper torso for each run.

A careful examination of these figures shows that there is very little difference between the results for the different initial head and neck inclination angles. However, there is a difference in the results for different initial torso inclination angles. Interestingly, it is seen in Figures 21., 25., and 29. that the smallest peak restoring force magnitude occurs with a  $45^{\circ}$  torso inclination angle. This is also the case for the magnitude of the restoring moment as seen in Figures 32., 35., and 38. Moreover, the peaks occur at approximately 40 and 80 milliseconds, which corresponds to peak values of the riser force components as seen in Figures 3., 4., and 5.

The fact that the initial torso inclination has a greater effect upon the head/neck dynamics than the head and neck inclination may not be surprising when one considers the relative magnitudes of the masses and inertias of the torso bodies and the head and neck. This may be discouraging for a parachutist, since control of the initial relative head and neck inclination is probably easier than control of the initial torso inclination. However, for designers of automatic parachute-opening devices for high-speed egress, these results may be encouraging, since torso inclination is likely to vary at a more uniform rate than the head and neck inclination.

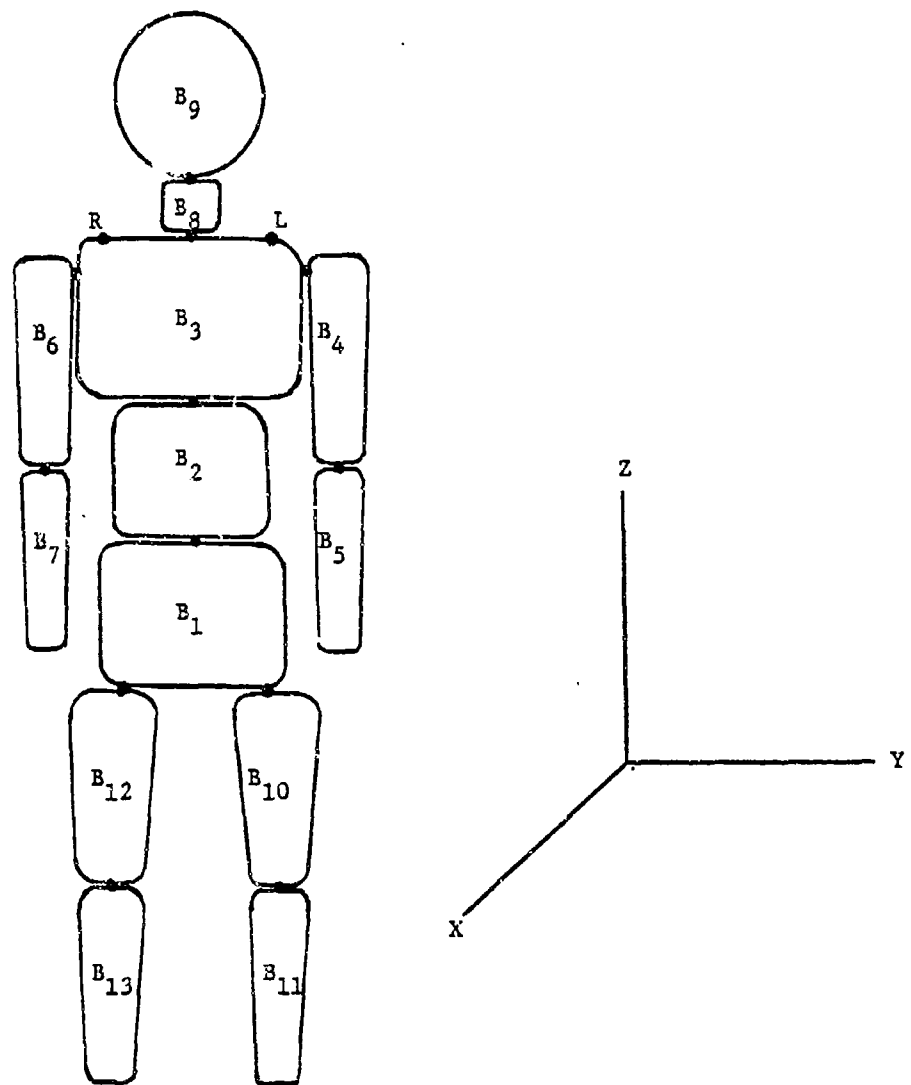


Figure 1. Biodynamic Model of a Parachutist

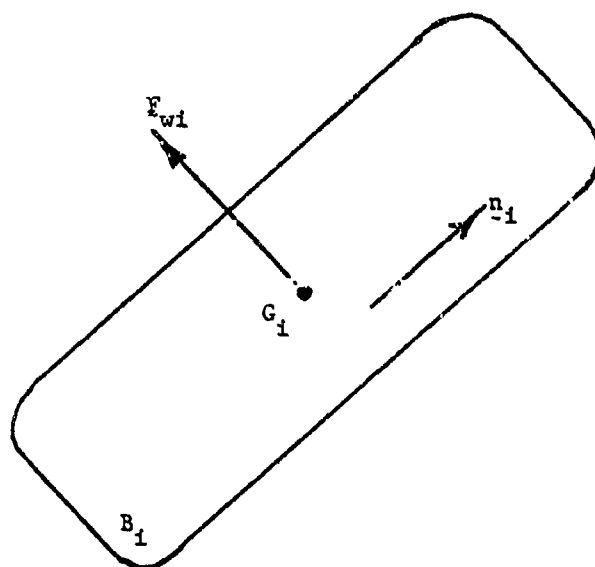


Figure 2. Air Drag Force on a Typical Body



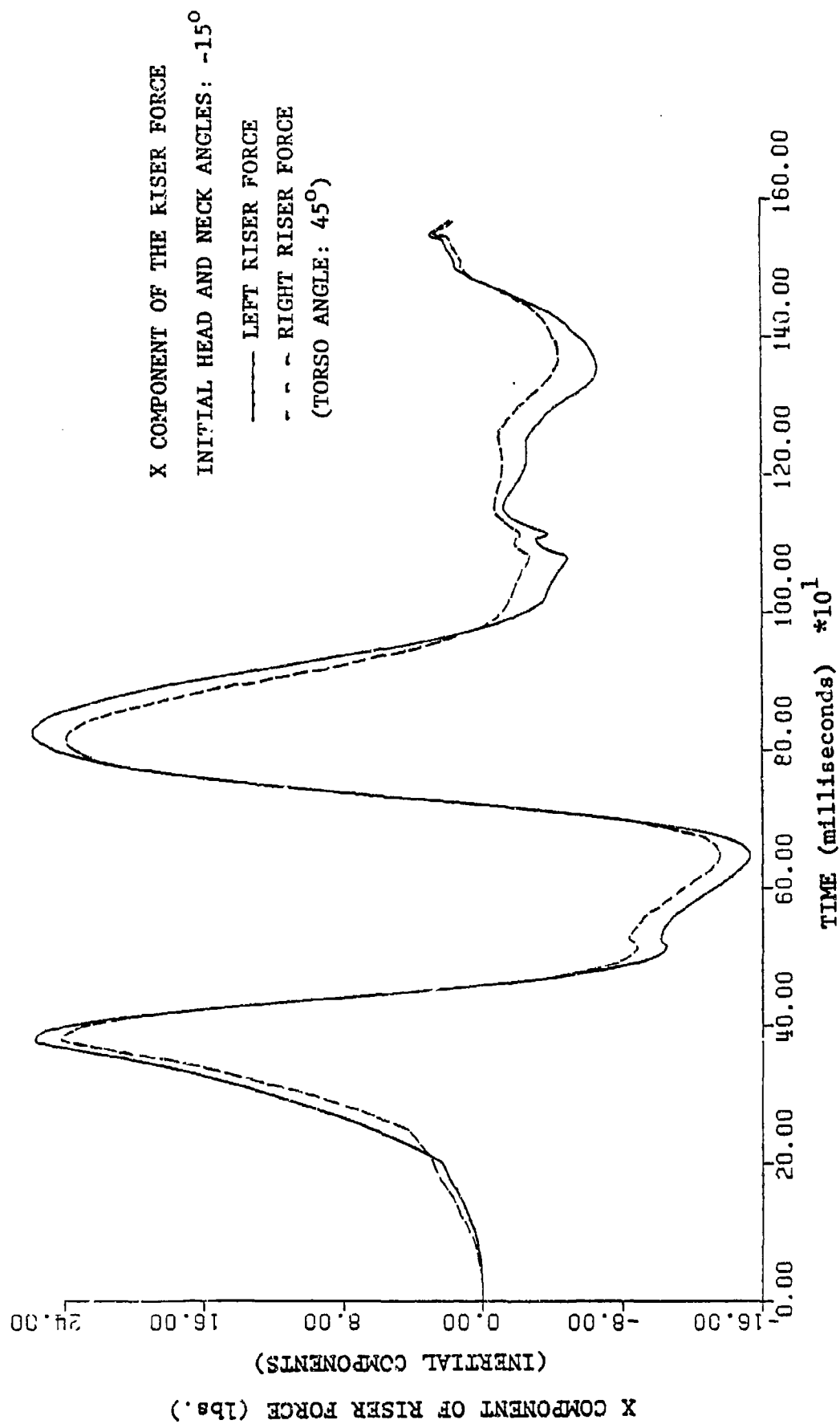


Figure 3. X Component of the Riser Force

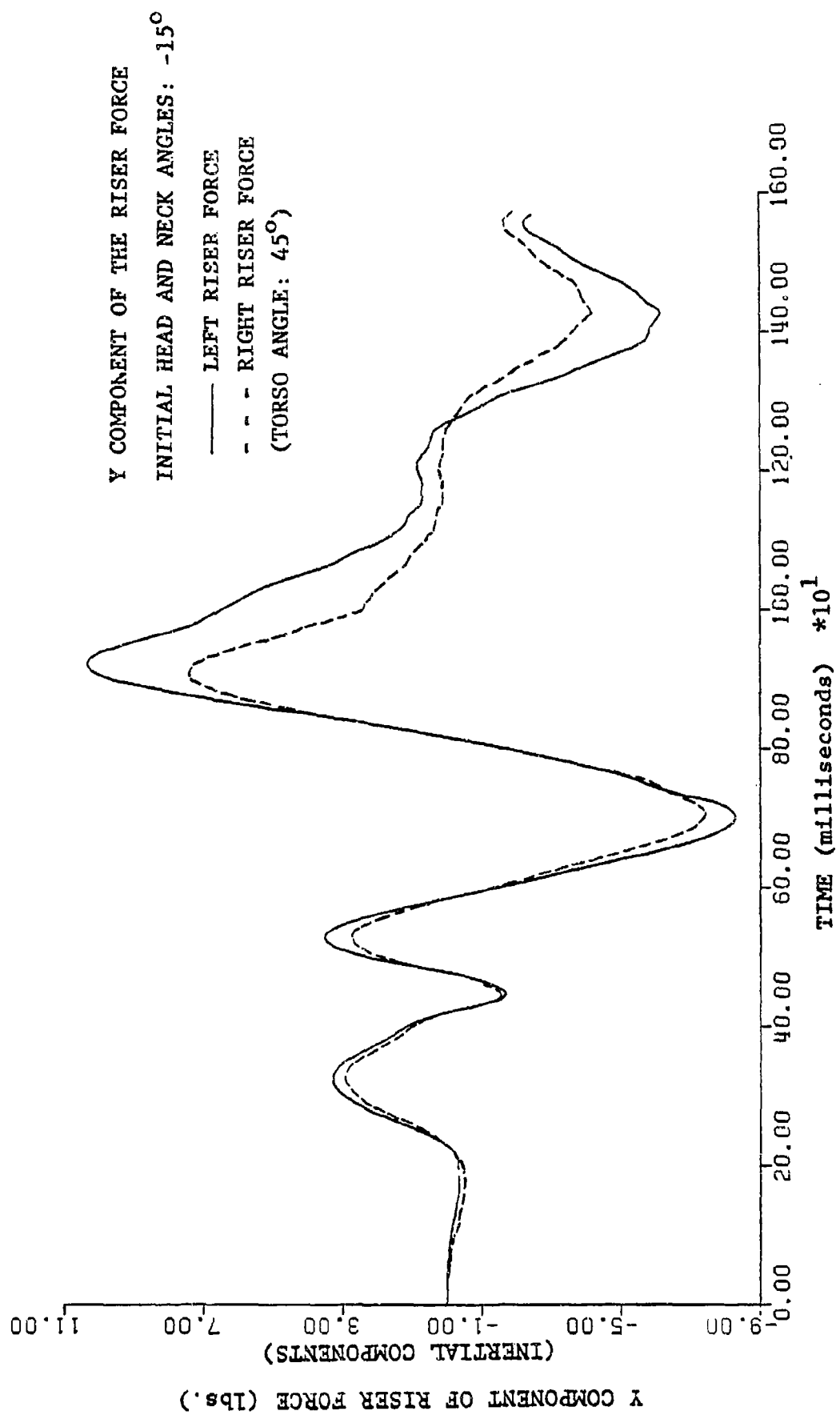


Figure 4. Y Component of the Riser Force

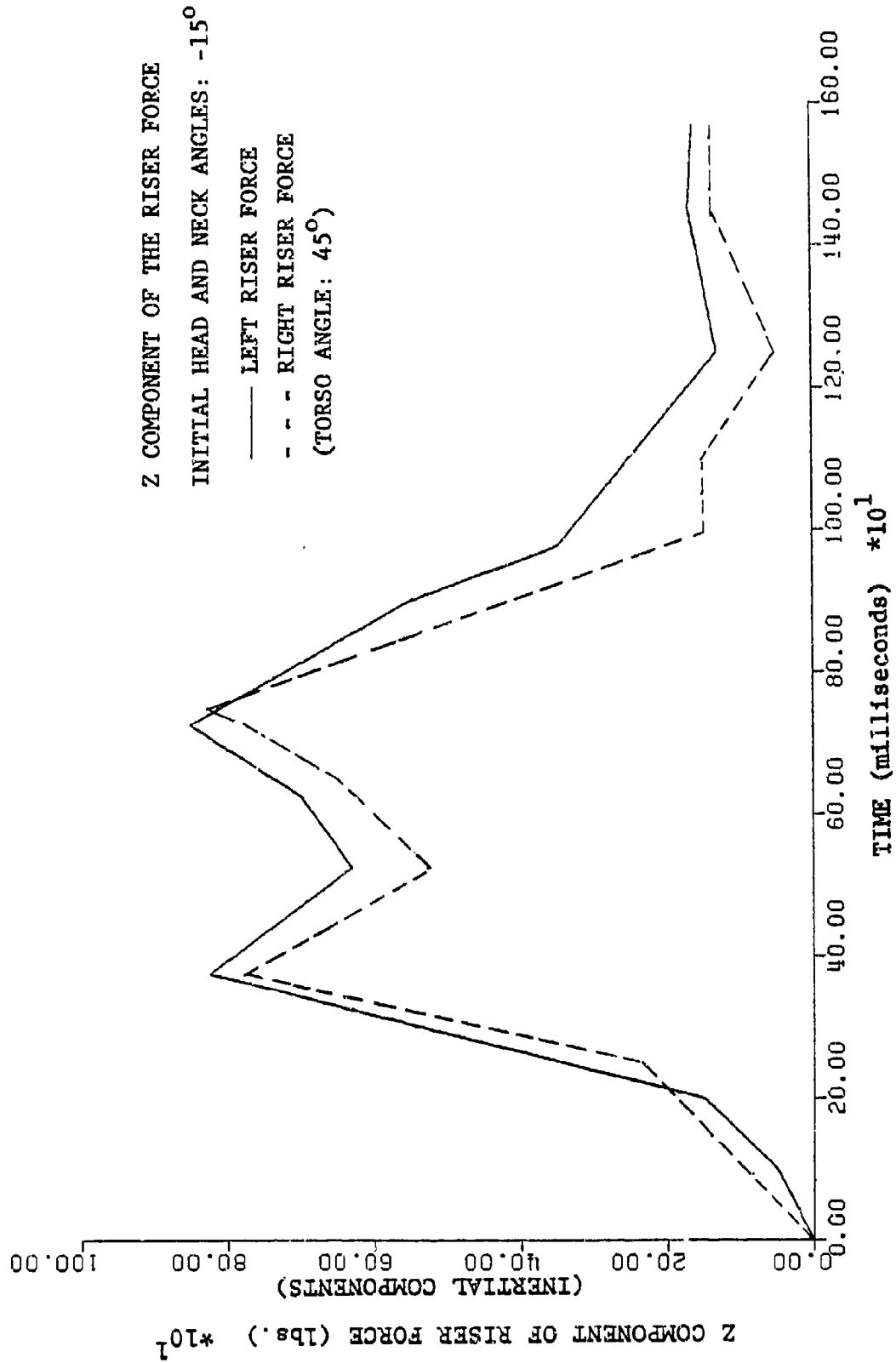


Figure 5. Z Component of the Riser Force

ALPHA ROTATION OF THE HEAD RELATIVE TO THE NECK

INITIAL HEAD AND NECK ANGLES:  $-15^{\circ}$

INITIAL ANGLE BETWEEN THE TORSO  
AND A VERTICAL LINE:

—  $67.5^{\circ}$   
- -  $45^{\circ}$   
- + -  $22.5^{\circ}$

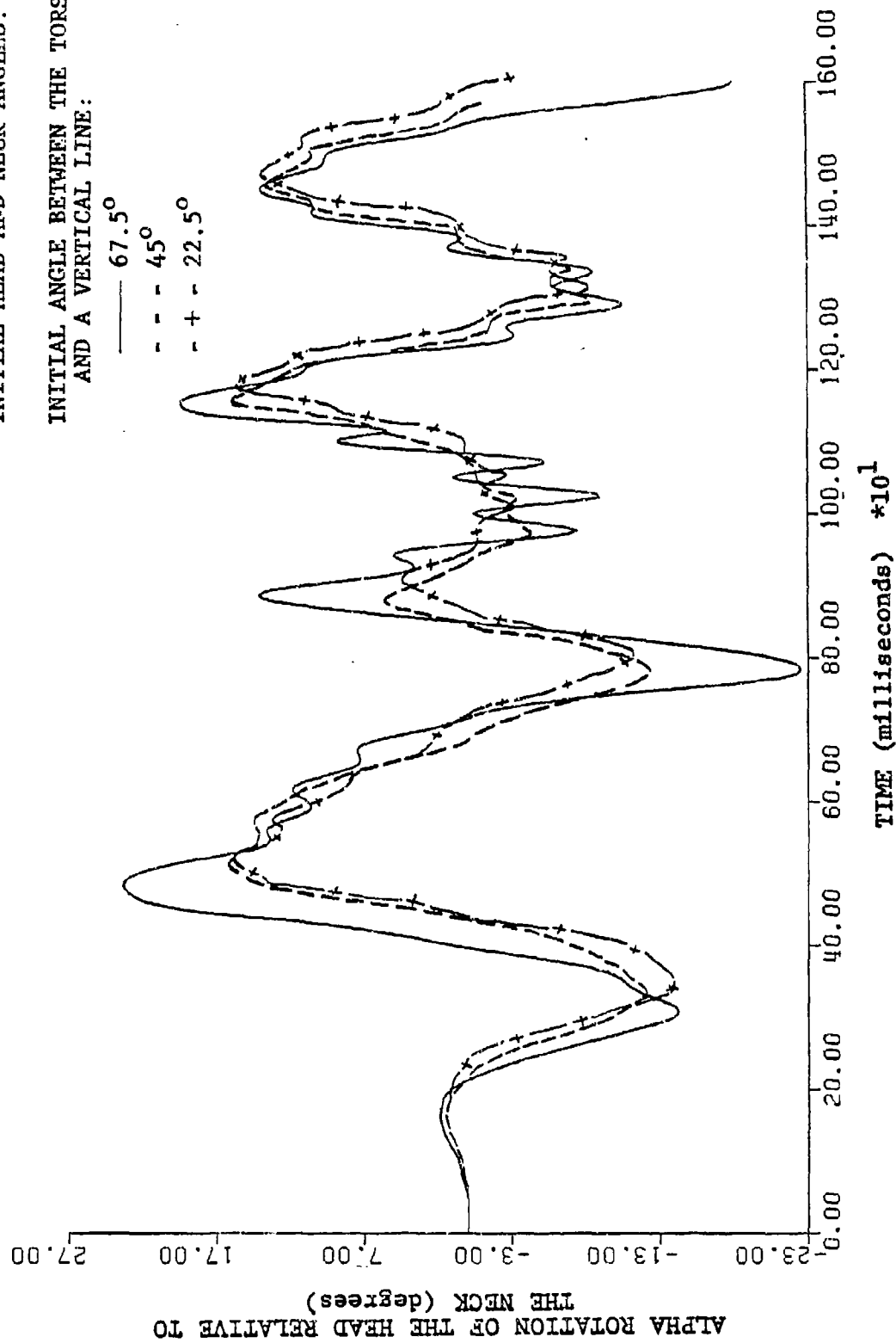


Figure 6. Alpha Rotation of the Head Relative to the Neck

BETA ROTATION OF THE HEAD RELATIVE TO THE NECK

INITIAL HEAD AND NECK ANGLES:  $-15^{\circ}$

INITIAL ANGLE BETWEEN THE TORSO  
AND A VERTICAL LINE:

—  $67.5^{\circ}$

- - -  $45^{\circ}$

- + -  $22.5^{\circ}$

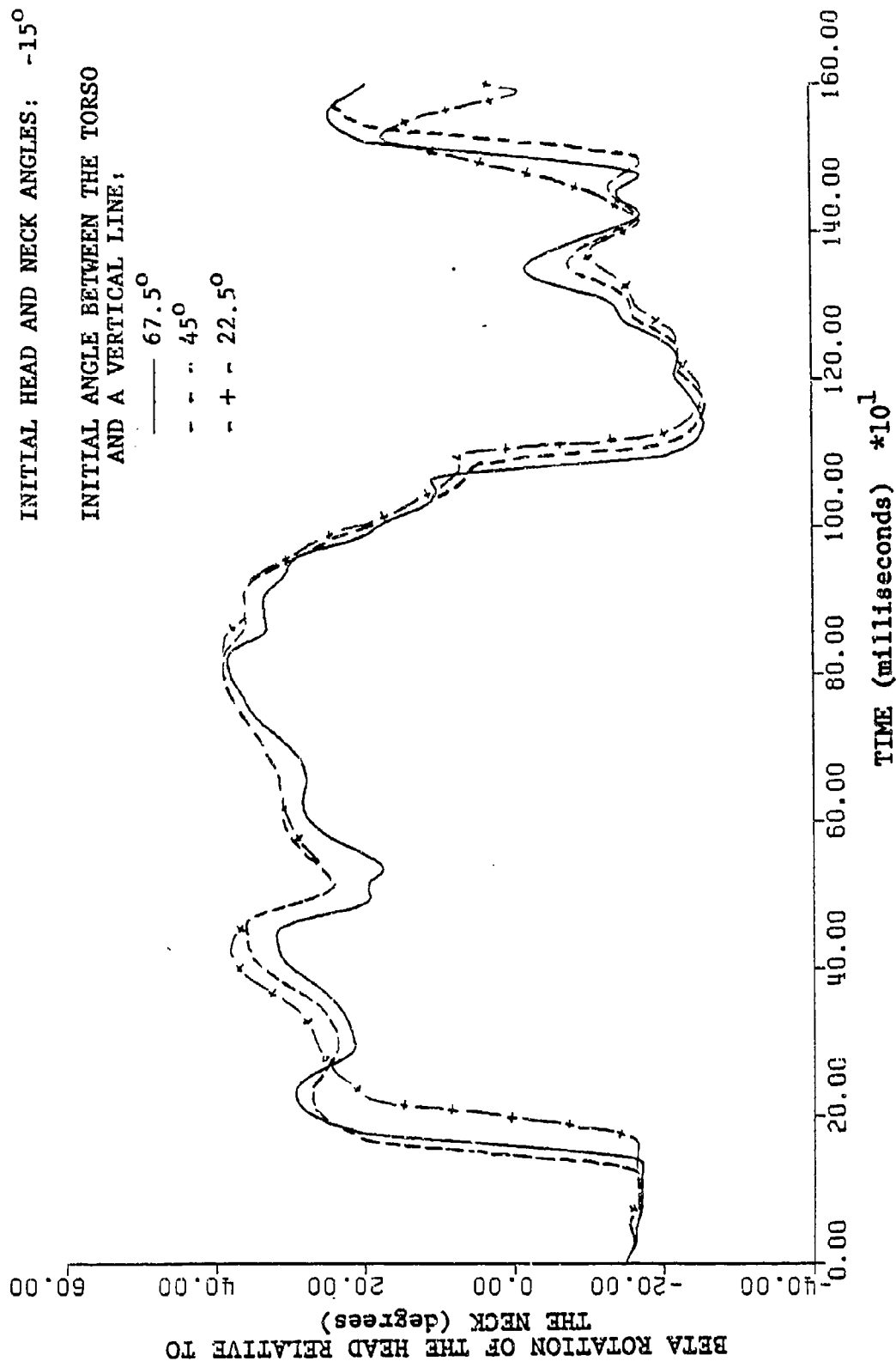


Figure 7. Beta Rotation of the Head Relative to the Neck

ALPHA ROTATION OF THE NECK RELATIVE TO THE TORSO  
 INITIAL HEAD AND NECK ANGLES;  $-15^{\circ}$   
 INITIAL ANGLE BETWEEN THE TORSO AND A VERTICAL LINE:

-----  $67.5^{\circ}$   
 - - - -  $45^{\circ}$   
 - + -  $22.5^{\circ}$

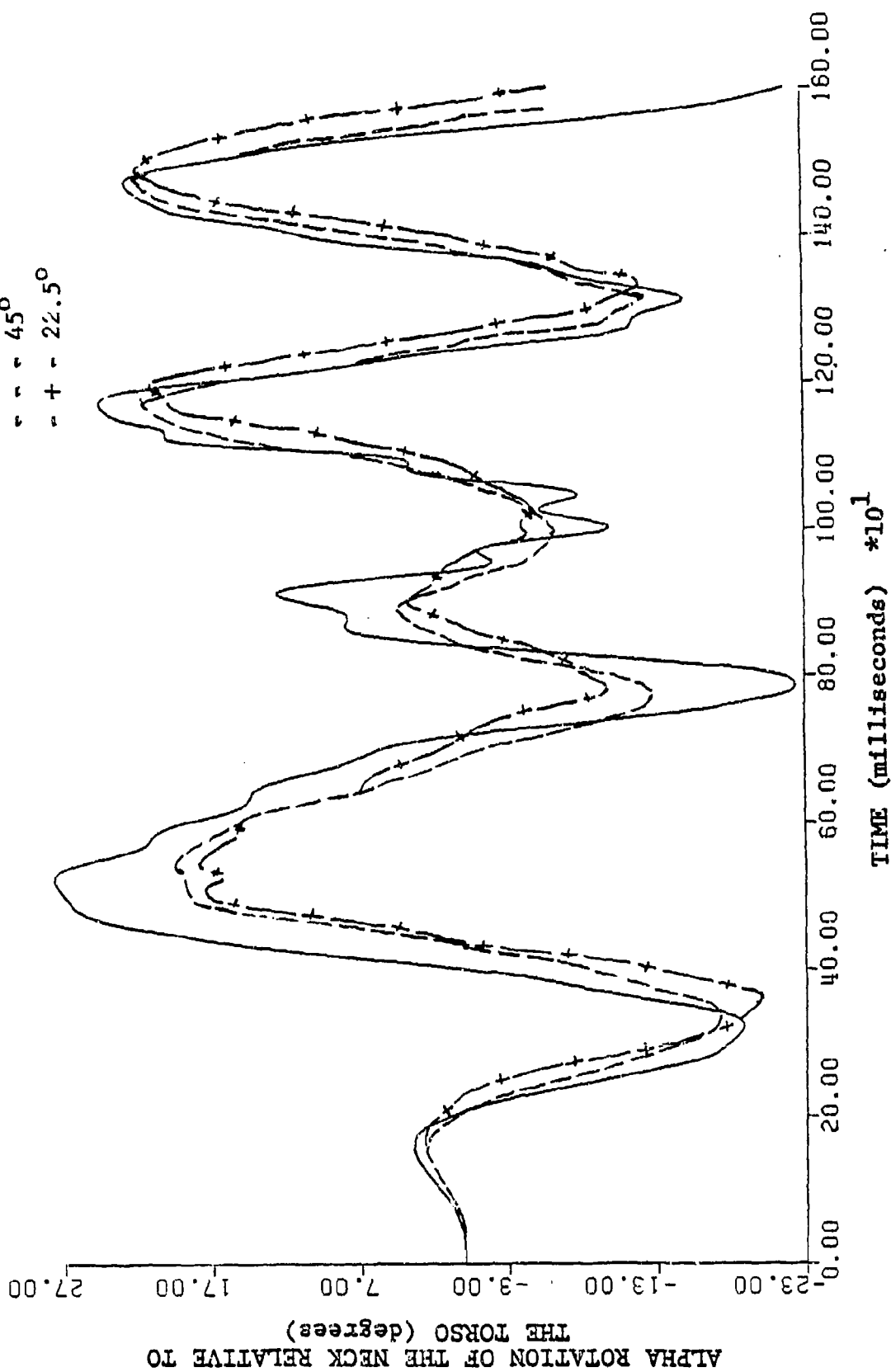


Figure 8. Alpha Rotation of the Neck Relative to the Torso

BETA ROTATION OF THE NECK RELATIVE TO THE TORSO

INITIAL HEAD AND NECK ANGLES:  $-15^{\circ}$

INITIAL ANGLE BETWEEN THE TORSO AND A VERTICAL LINE:

-----  $67.5^{\circ}$

- - - -  $45^{\circ}$

- + -  $22.5^{\circ}$

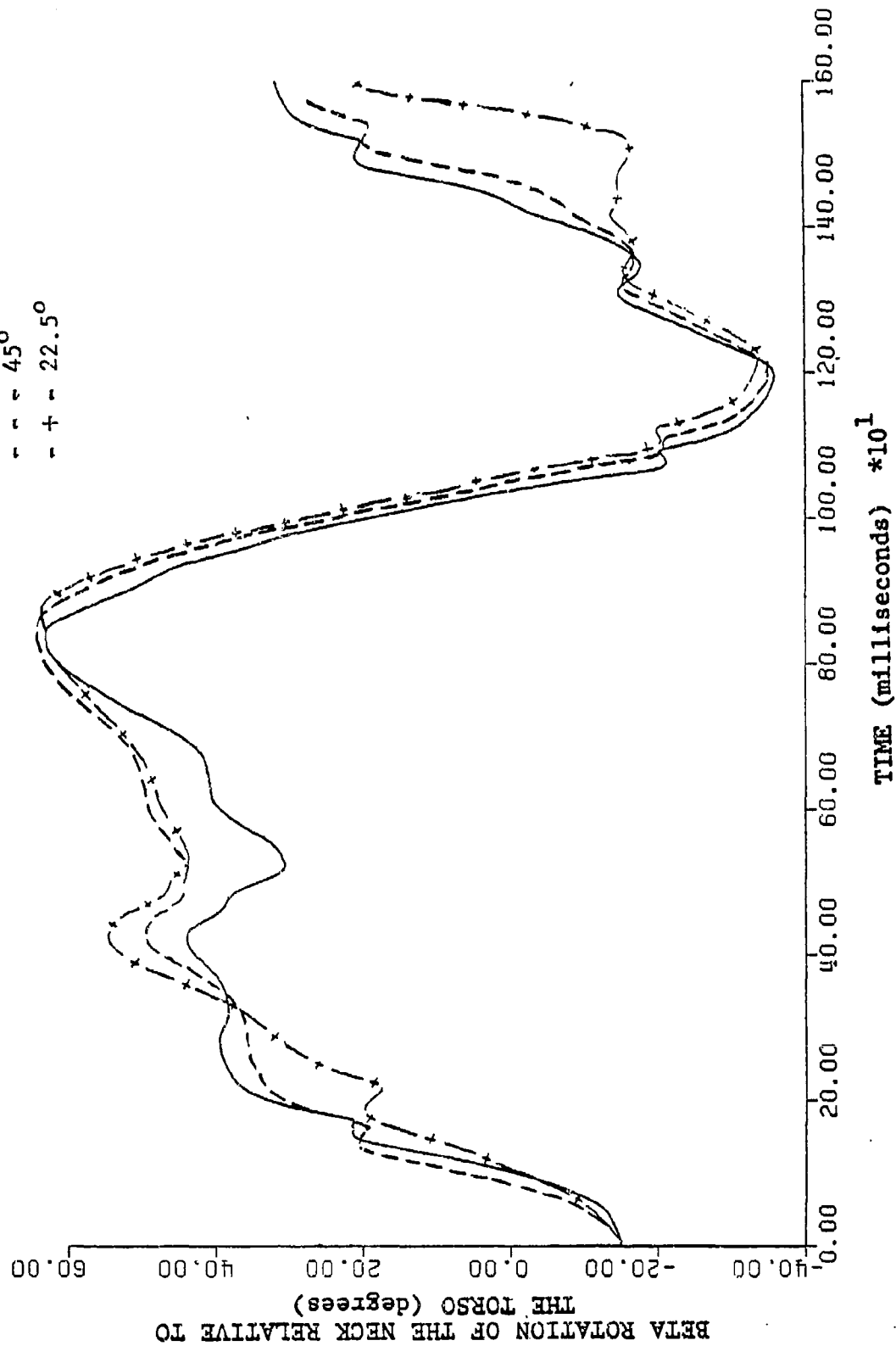


Figure 9, Beta Rotation of the Neck Relative to the Torso

ALPHA ROTATION OF THE HEAD RELATIVE TO THE NECK

INITIAL HEAD AND NECK ANGLES:  $0^{\circ}$

INITIAL ANGLE BETWEEN THE TORSO AND A VERTICAL LINE:

--- 67.5°

- - - 45°

- + - 22.5°

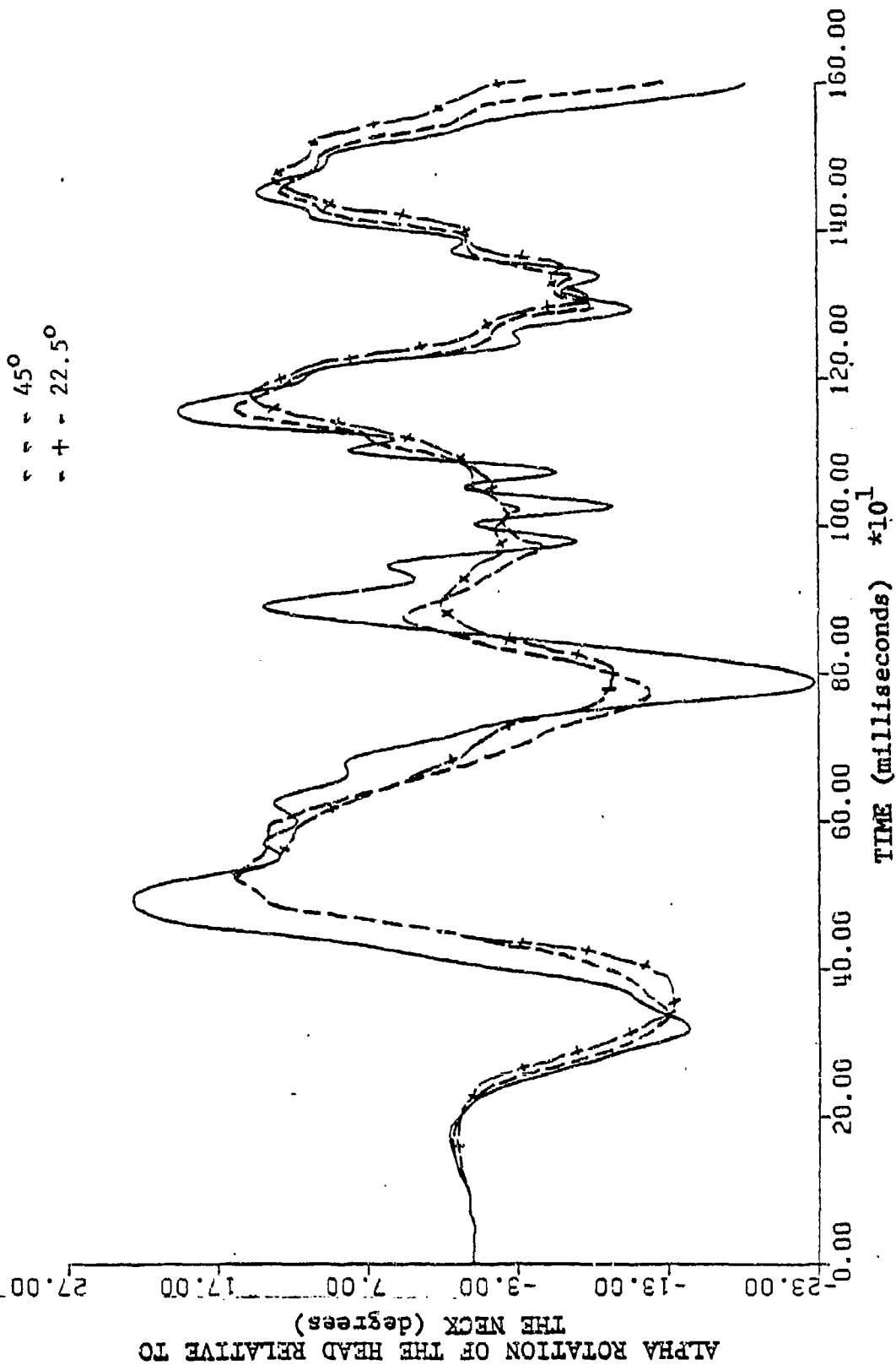


Figure 10. Alpha Rotation of the Head Relative to the Neck



BETA ROTATION OF THE HEAD RELATIVE TO THE NECK  
 INITIAL HEAD AND NECK ANGLES:  $0^{\circ}$   
 INITIAL ANGLE BETWEEN THE TORSO AND A VERTICAL LINE:

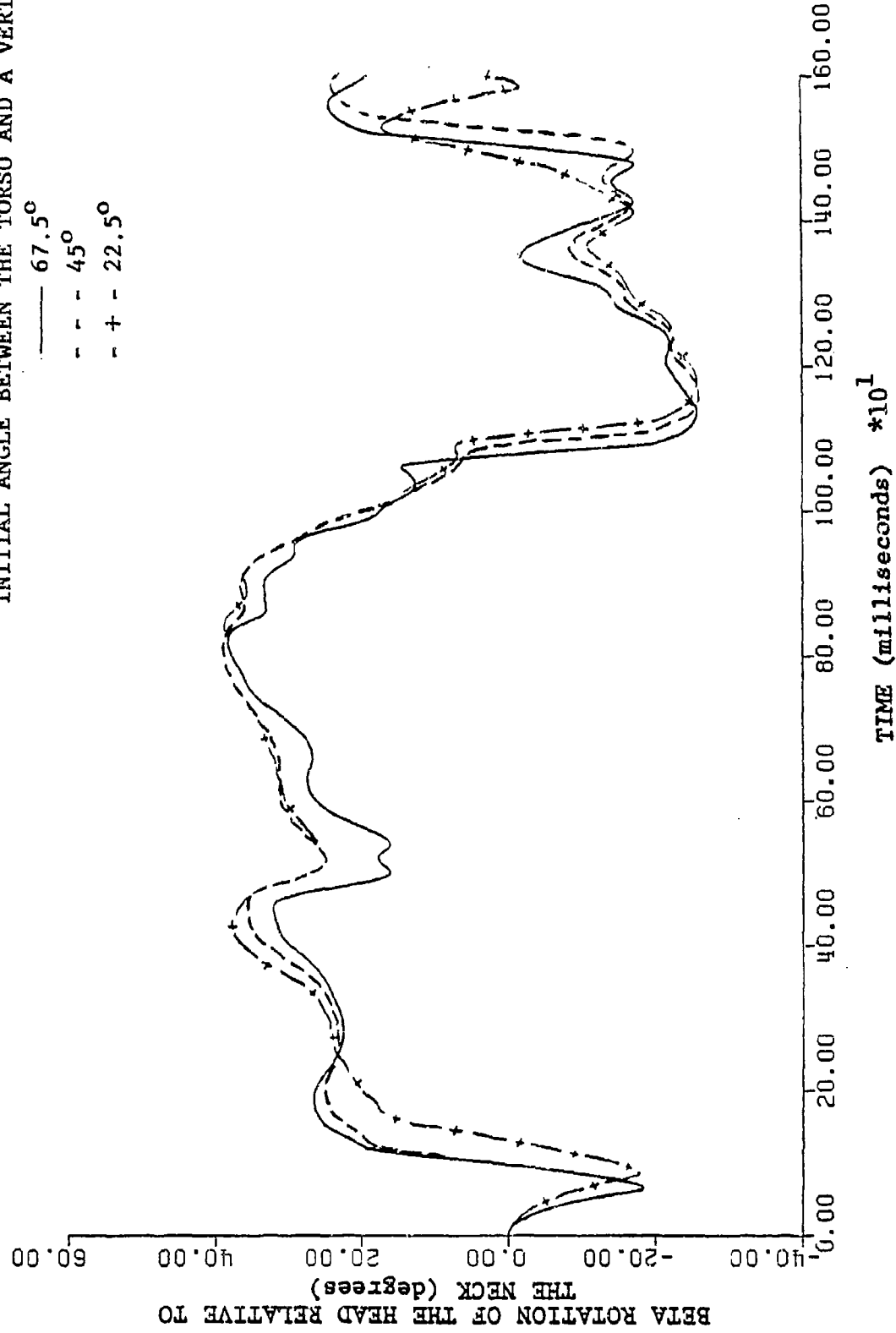


Figure 11. Beta Rotation of the Head Relative to the Neck

ALPHA ROTATION OF THE NECK RELATIVE TO THE TORSO

INITIAL HEAD AND NECK ANGLES:  $0^{\circ}$

INITIAL ANGLE BETWEEN THE TORSO AND A VERTICAL LINE:

--- 67.5°

- - - 45°

- + - 22.5°

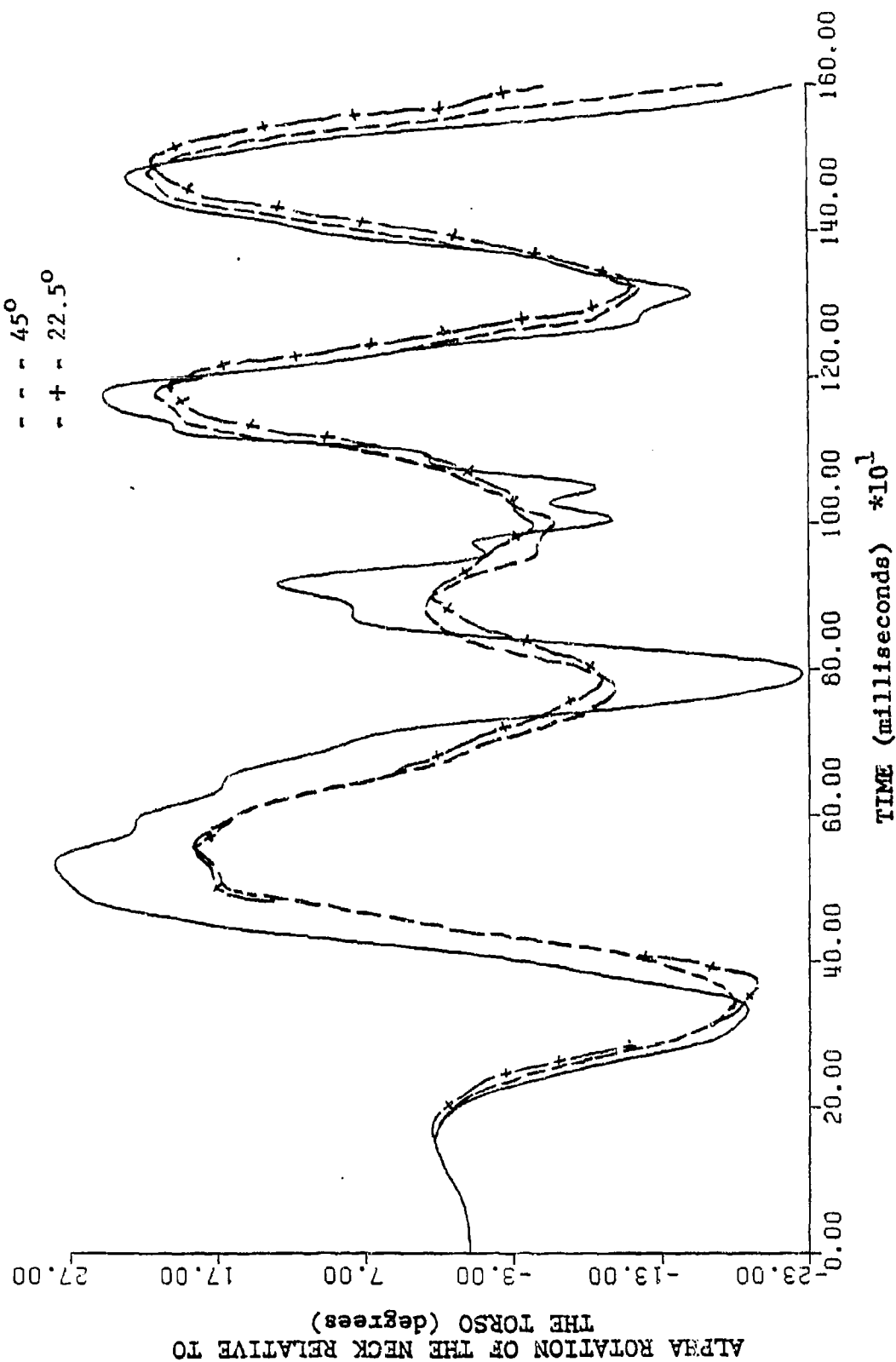


Figure 12. Alpha Rotation of the Neck Relative to the Torso

BETA ROTATION OF THE NECK RELATIVE TO THE TORSO

INITIAL HEAD AND NECK ANGLES:  $0^{\circ}$

INITIAL ANGLE BETWEEN THE TORSO AND A VERTICAL LINE:

— 67.5°

- - - 45°

- + - 22.5°

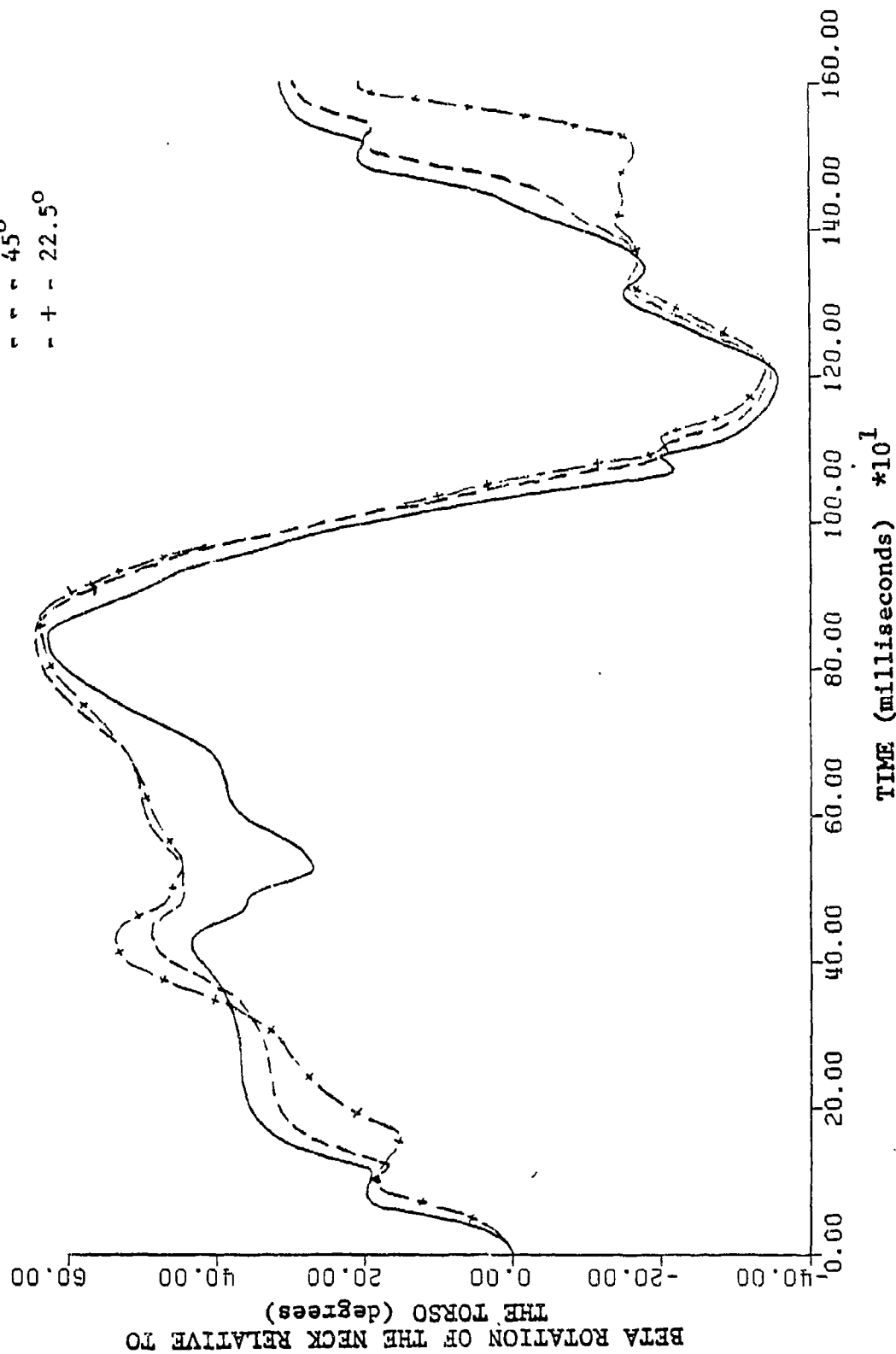


Figure 13. Beta Rotation of the Neck Relative to the Torso

ALPHA ROTATION OF THE HEAD RELATIVE TO THE NECK  
 INITIAL HEAD AND NECK ANGLES:  $15^{\circ}$   
 INITIAL ANGLE BETWEEN THE TORSO AND A VERTICAL LINE:

—  $67.5^{\circ}$   
 - -  $45^{\circ}$   
 - + -  $22.5^{\circ}$

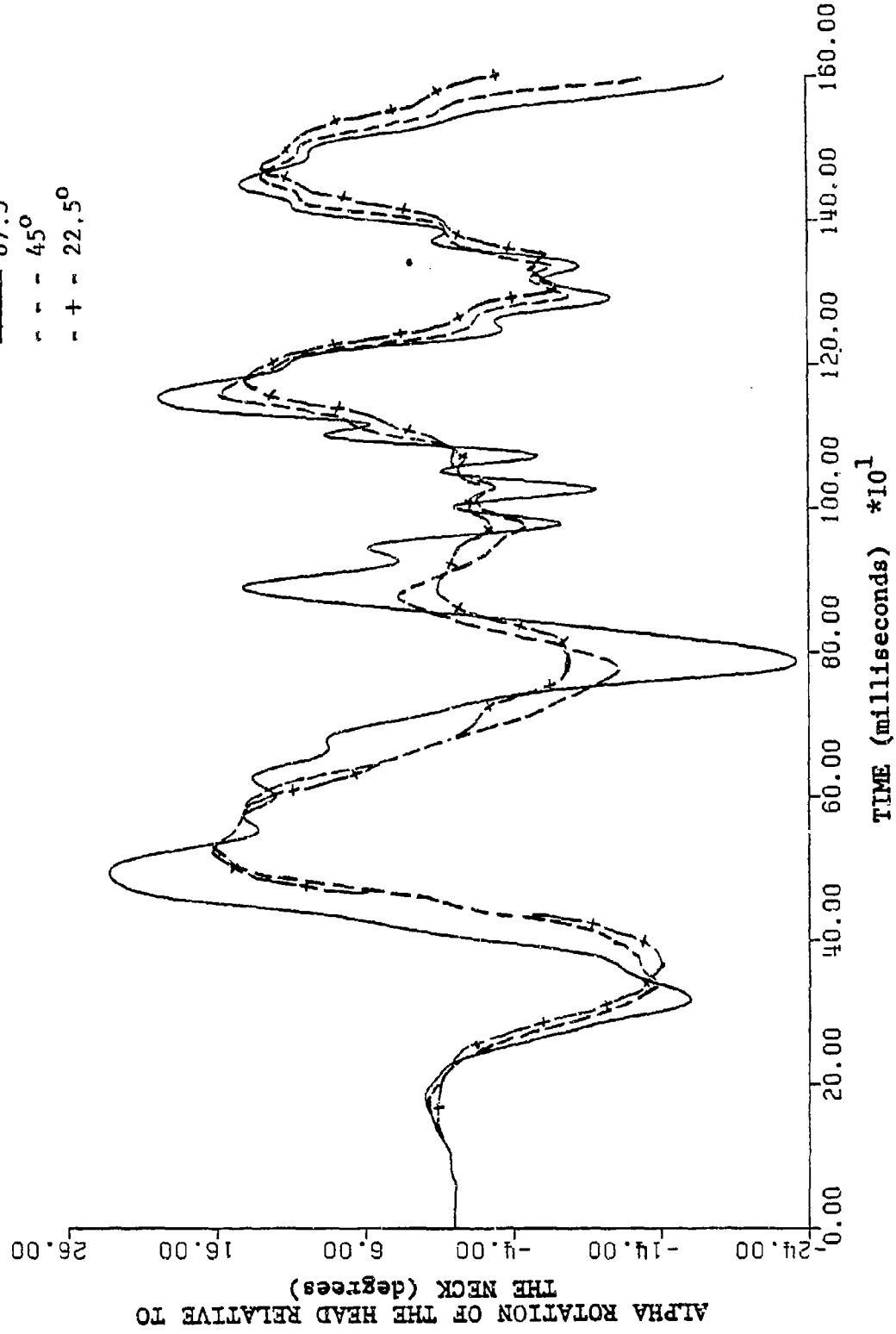


Figure 14. Alpha Rotation of the Head Relative to the Neck

BETA ROTATION OF THE HEAD RELATIVE TO THE NECK

INITIAL HEAD AND NECK ANGLES:  $15^{\circ}$

INITIAL ANGLE BETWEEN THE TORSO AND A VERTICAL LINE:

-----  $67.5^{\circ}$

- - - - -  $45^{\circ}$

+ + + + +  $22.5^{\circ}$

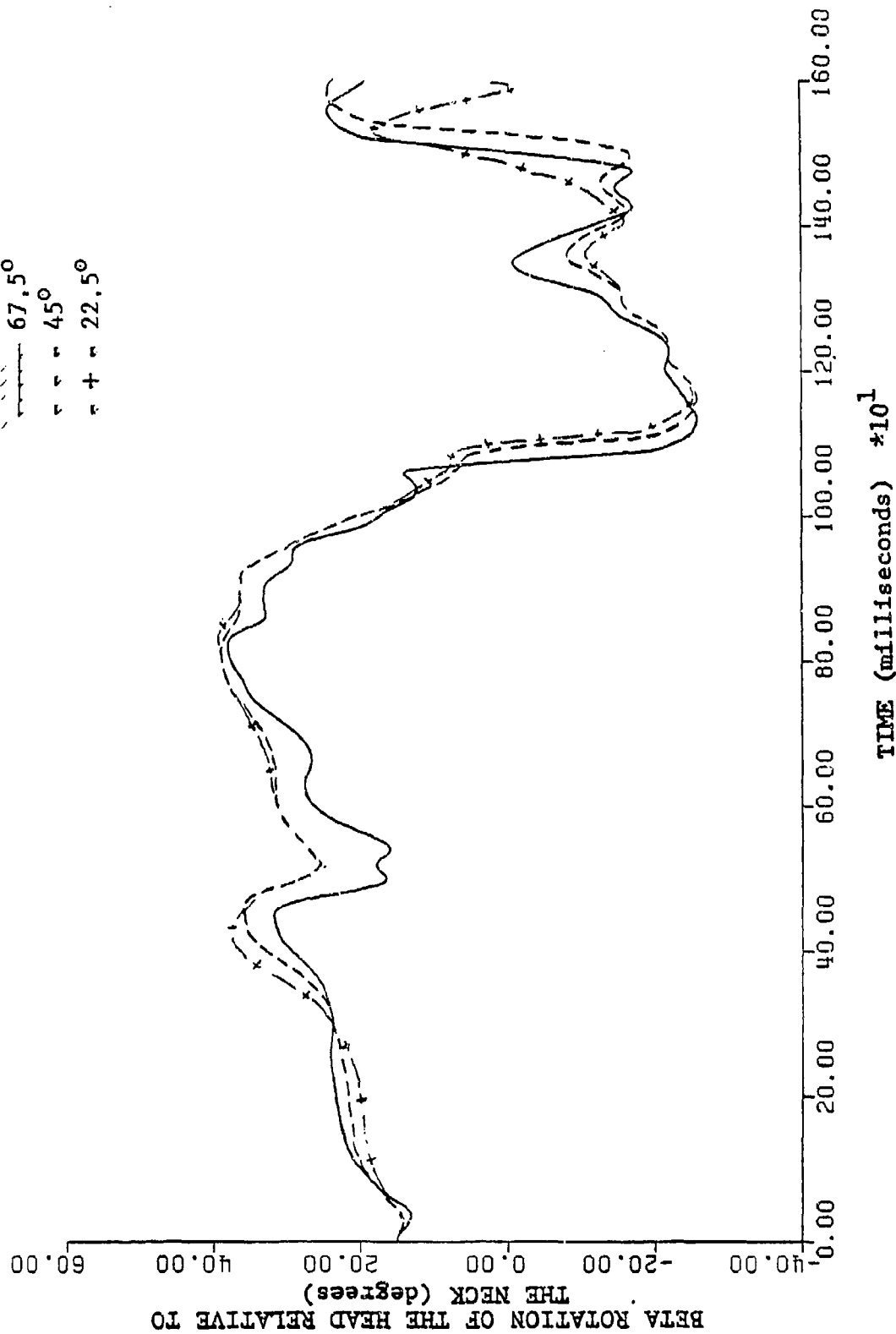


Figure 15, Beta Rotation of the Head Relative to the Neck

ALPHA ROTATION OF THE NECK RELATIVE TO THE TORSO  
 INITIAL HEAD AND NECK ANGLES;  $15^{\circ}$   
 INITIAL ANGLE BETWEEN THE TORSO AND A VERTICAL LINE:

— 67.5°  
 - - - 45°  
 - + - 22.5°

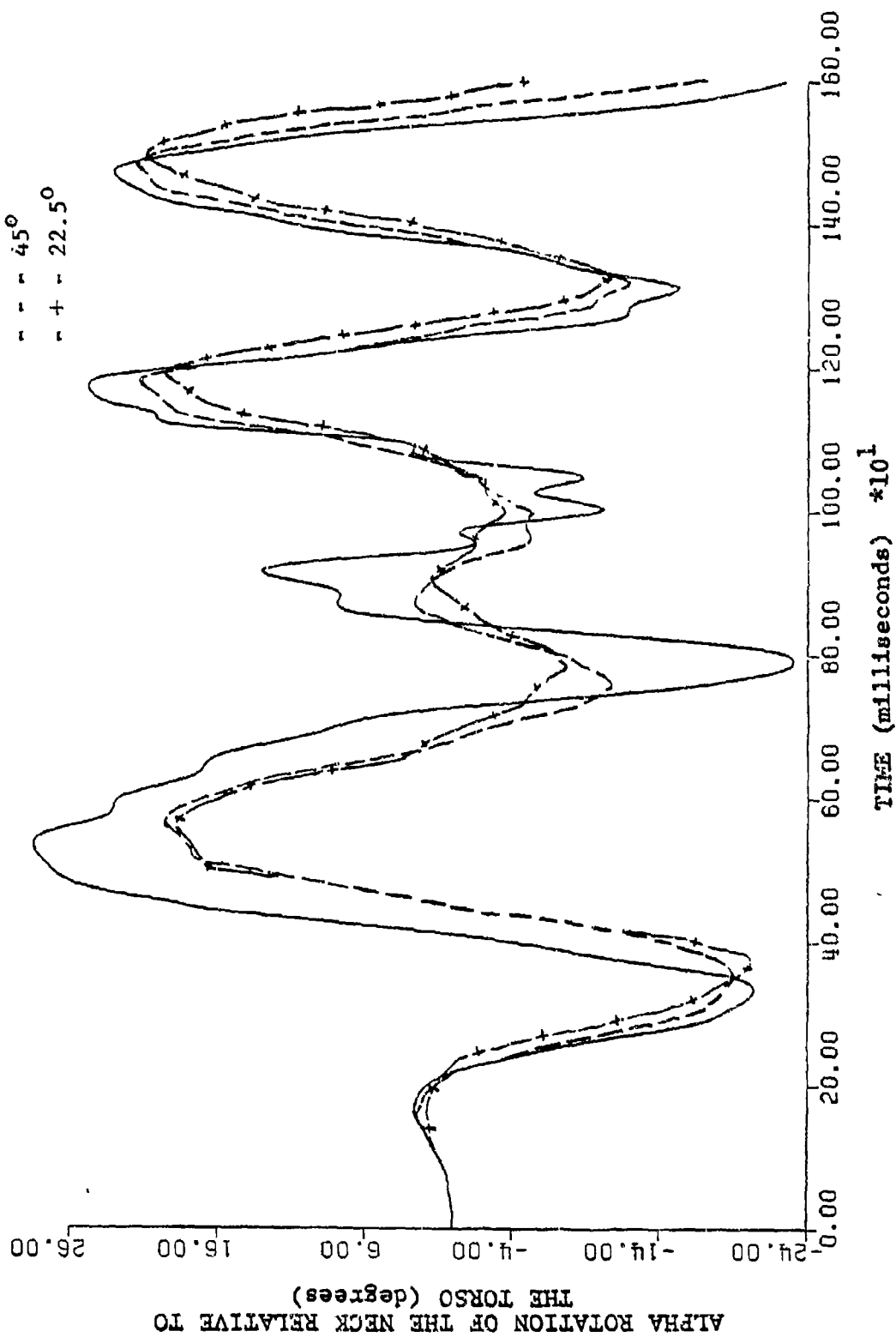


Figure 16. Alpha Rotation of the Neck Relative to the Torso

BETA ROTATION OF THE NECK RELATIVE TO THE TORSO  
 INITIAL HEAD AND NECK ANGLES:  $15^{\circ}$   
 INITIAL ANGLE BETWEEN THE TORSO AND A VERTICAL LINE:

—  $67.5^{\circ}$   
 - - -  $45^{\circ}$   
 - + -  $22.5^{\circ}$

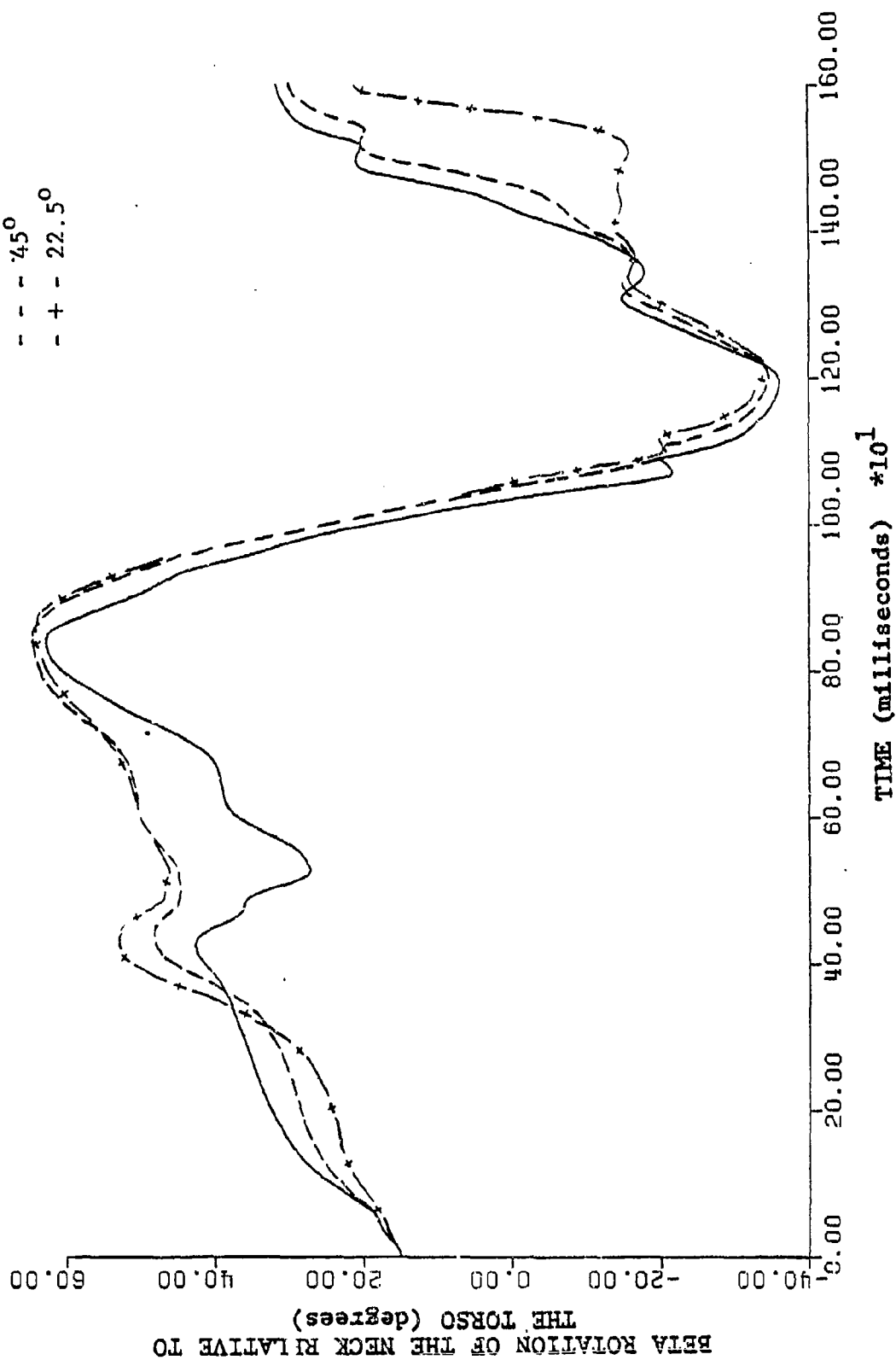


Figure 17. Beta Rotation of the Neck Relative to the Torso

X COMPONENT OF THE CONSTRAINT FORCE  
BETWEEN THE HEAD AND THE NECK

INITIAL HEAD AND NECK ANGLES:  $-15^{\circ}$

INITIAL ANGLE BETWEEN THE TORSO  
AND A VERTICAL LINE:

— 67.5°  
-- 45°  
- + - 22.5°

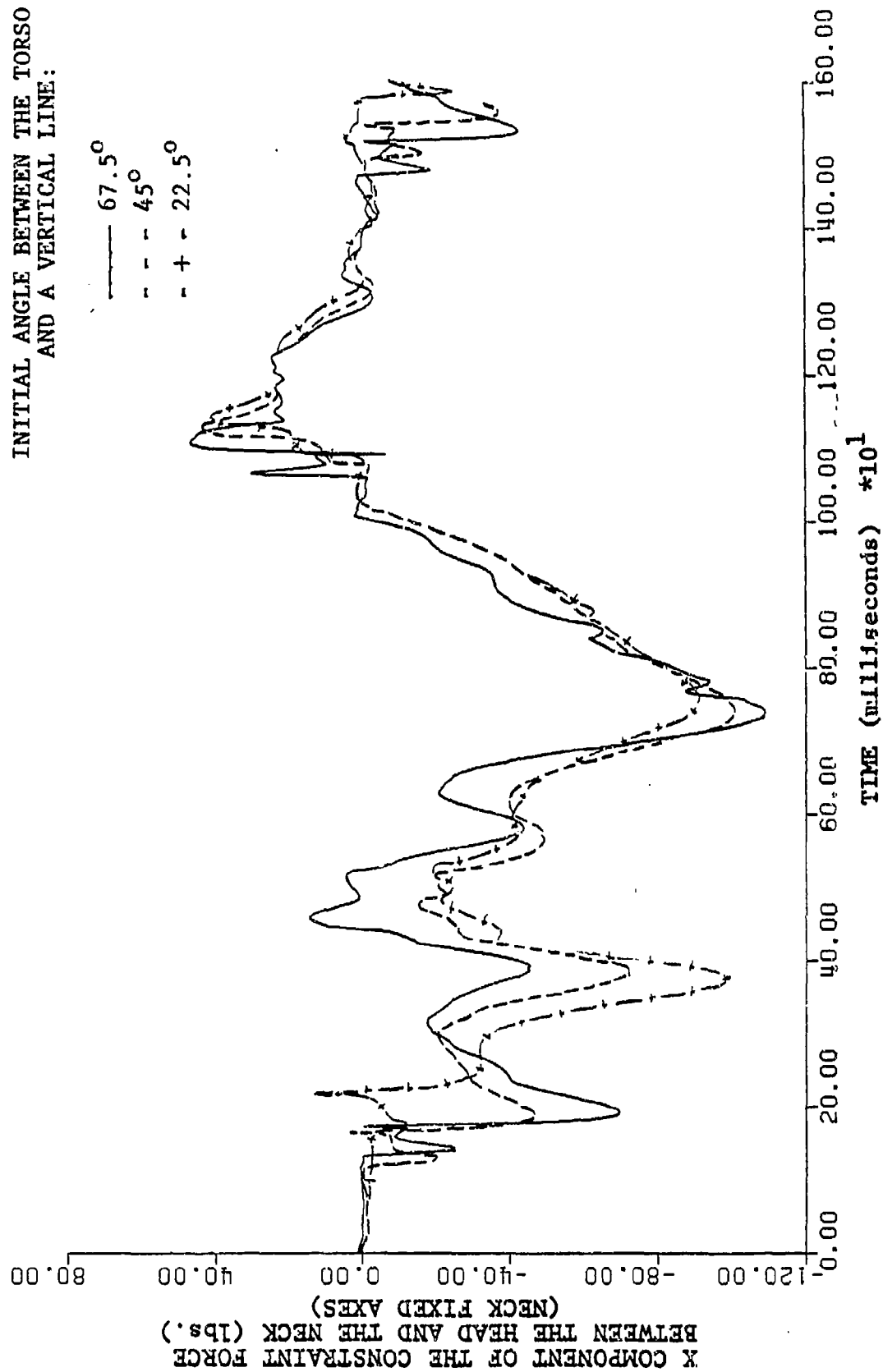


Figure 18. X Component of the Constraint Force Between the Head and the Neck



Y COMPONENT OF THE CONSTRAINT FORCE  
BETWEEN THE HEAD AND THE NECK

INITIAL HEAD AND NECK ANGLES:  $-15^{\circ}$

INITIAL ANGLE BETWEEN THE TORSO  
AND A VERTICAL LINE:

— 67.5°  
- - - 45°  
- + - 22.5°

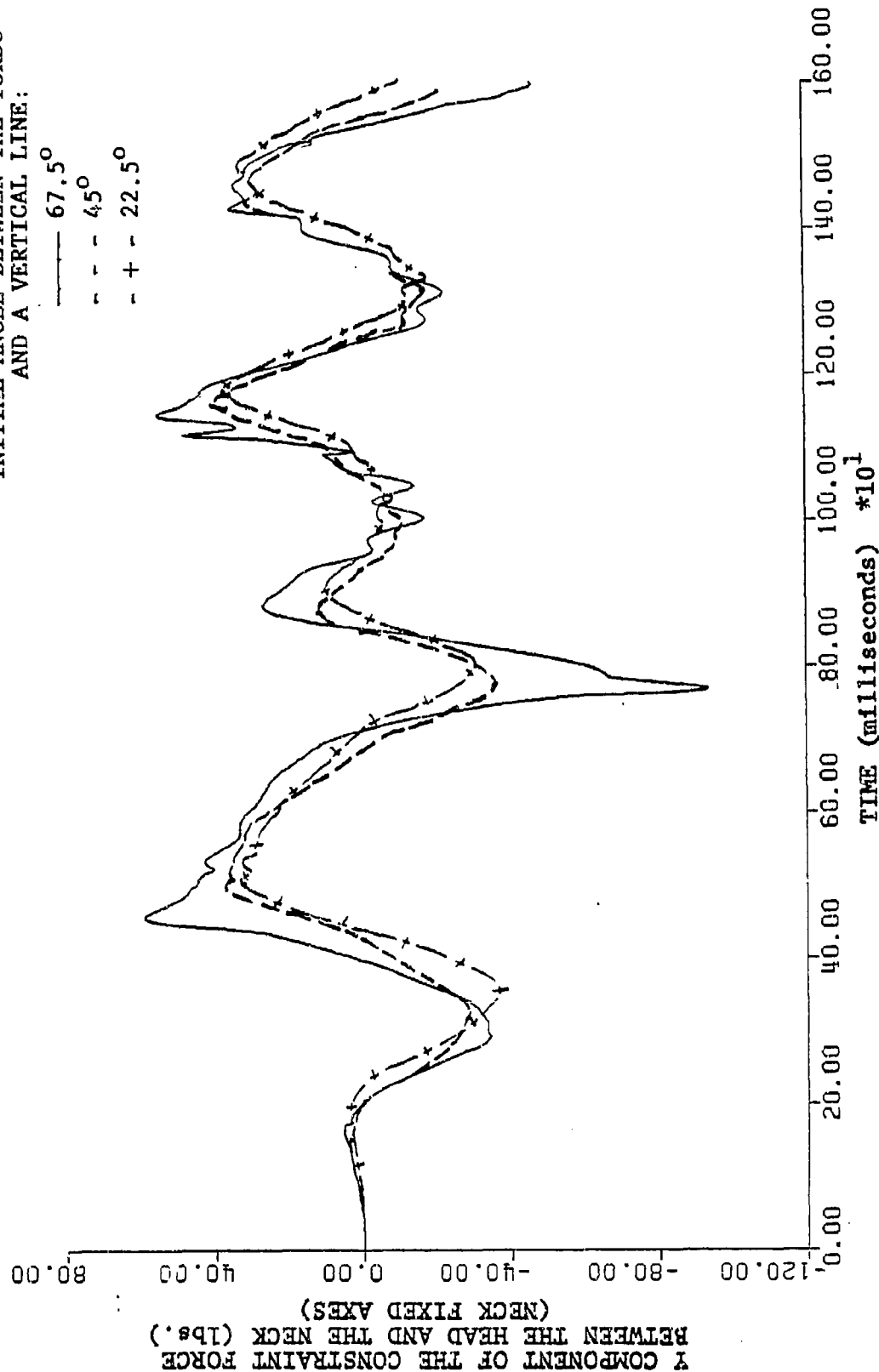


Figure 19, Y Component of the Constraint Force Between the Head and the Neck

Z COMPONENT OF THE CONSTRAINT FORCE  
BETWEEN THE HEAD AND THE NECK

INITIAL HEAD AND NECK ANGLES:  $-15^{\circ}$

INITIAL ANGLE BETWEEN THE TORSO  
AND A VERTICAL LINE:

— 67.5°  
- - - 45°  
+ + - 22.5°

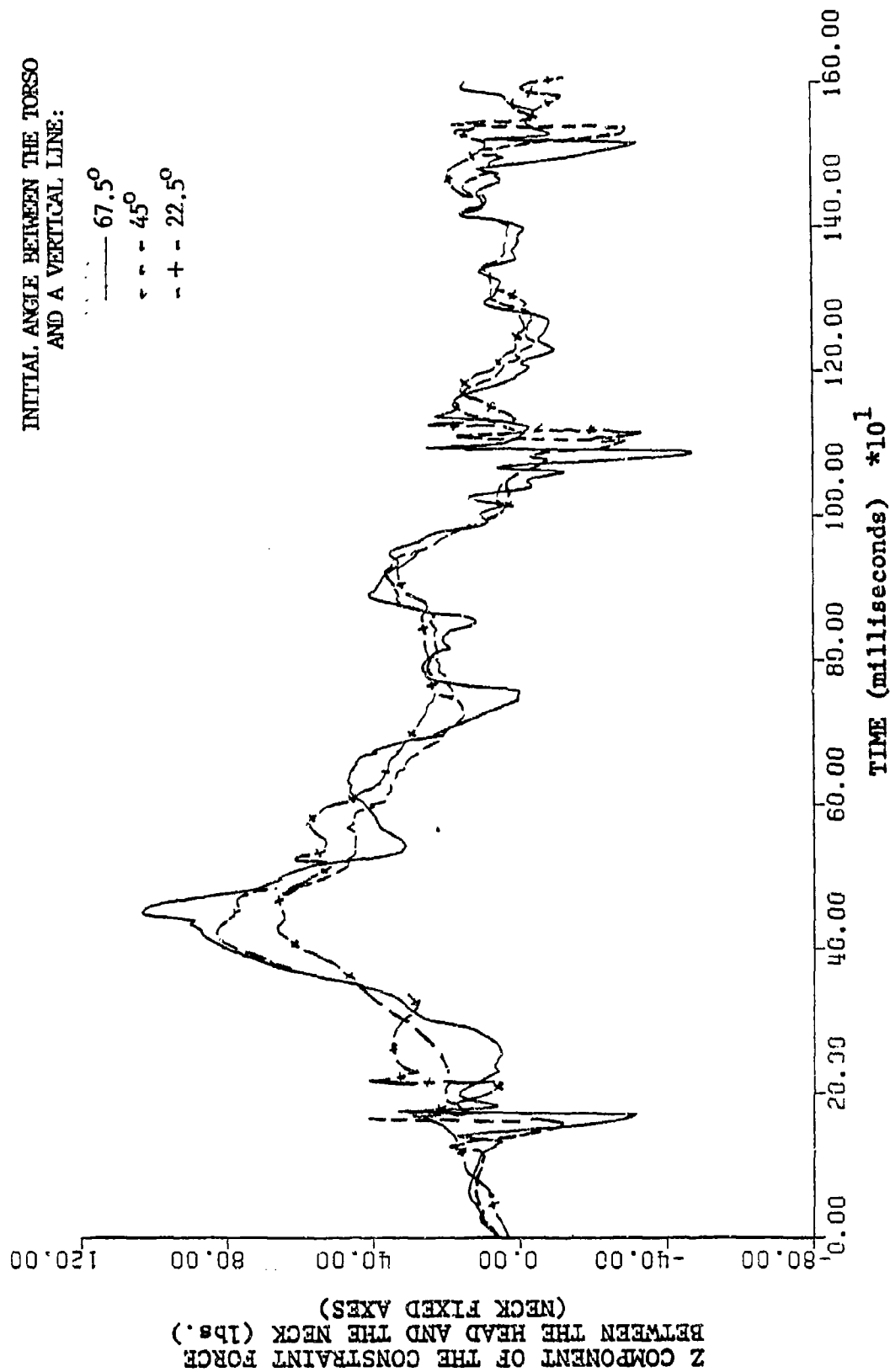


Figure 20. Z Component of the Constraint Force Between the Head and the Neck

MAGNITUDE OF THE CONSTRAINT FORCE BETWEEN  
THE HEAD AND THE NECK

INITIAL HEAD AND NECK ANGLES:  $-15^{\circ}$

INITIAL ANGLE BETWEEN THE TORSO  
AND A VERTICAL LINE:

—  $67.5^{\circ}$   
- - -  $45^{\circ}$   
- + -  $22.5^{\circ}$

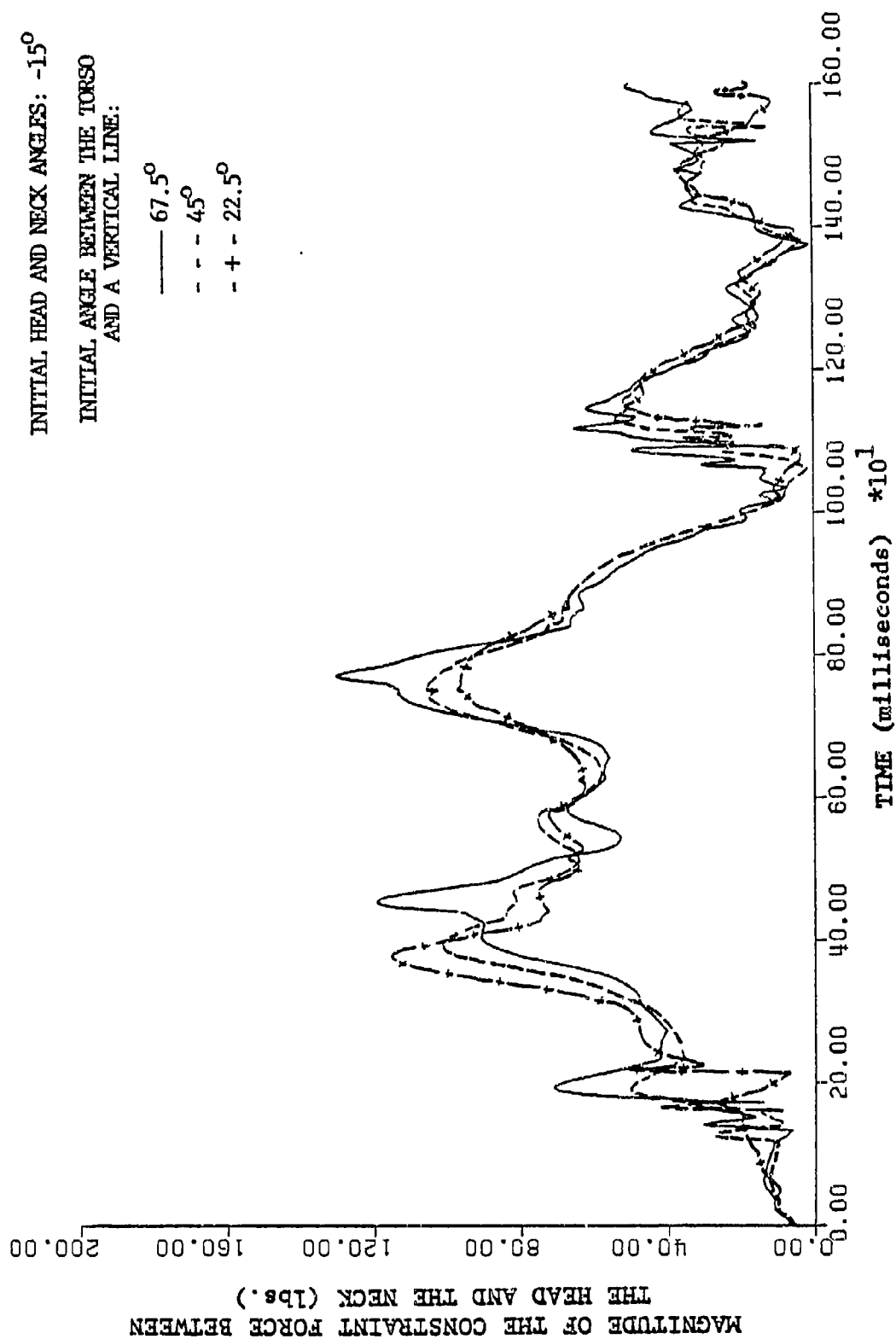


Figure 21. Magnitude of the Constraint Force Between the Head and the Neck

X COMPONENT OF THE CONSTRAINT FORCE  
BETWEEN THE HEAD AND THE NECK

INITIAL HEAD AND NECK ANGLES:  $0^{\circ}$

INITIAL ANGLE BETWEEN THE TORSO  
AND A VERTICAL LINE:

—  $67.5^{\circ}$   
- - -  $45^{\circ}$   
- + -  $22.5^{\circ}$

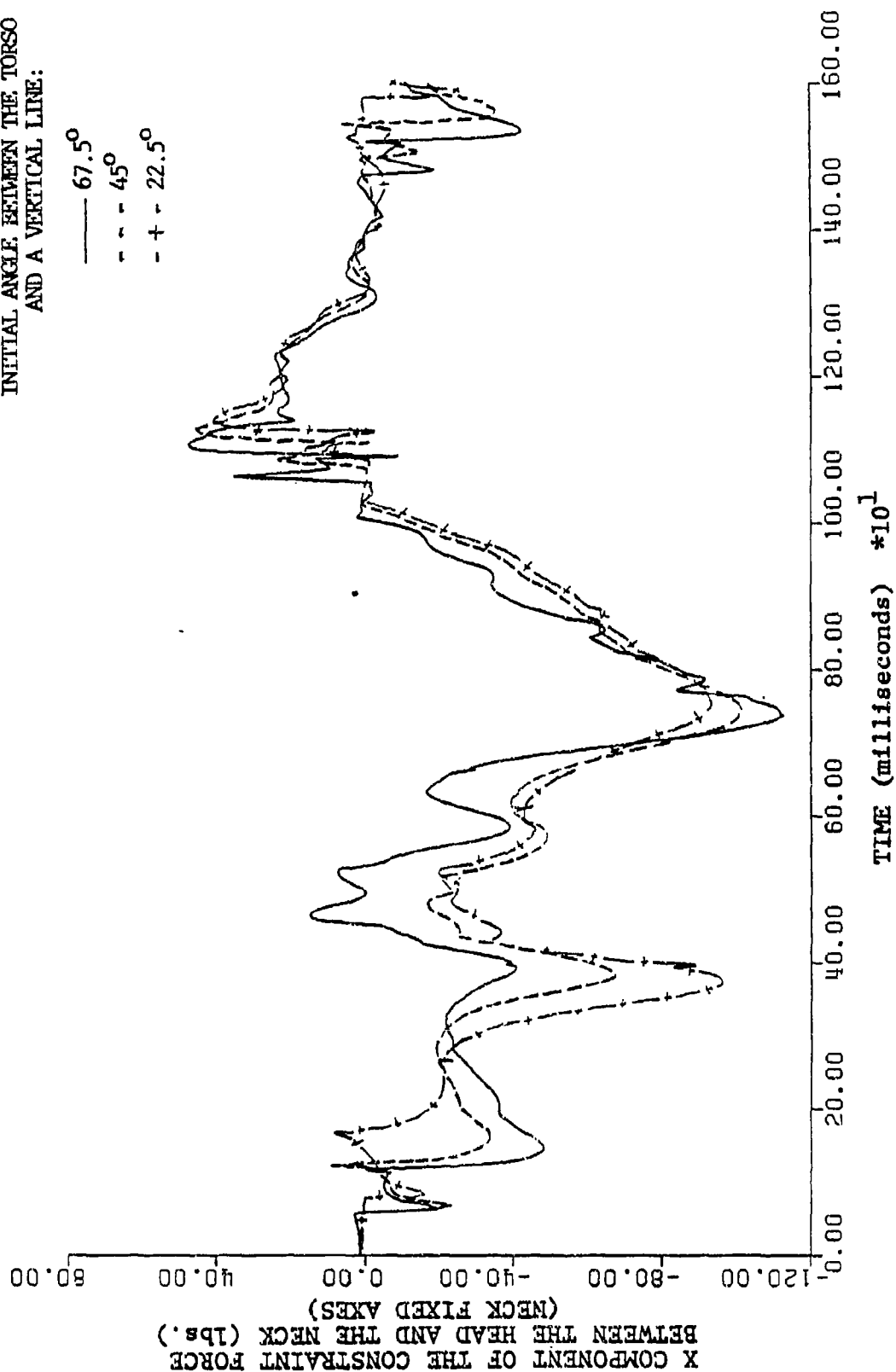


Figure 22. X Component of the Constraint Force Between the Head and the Neck

Y COMPONENT OF THE CONSTRAINT FORCE  
BETWEEN THE HEAD AND THE NECK

INITIAL HEAD AND NECK ANGLES:  $0^{\circ}$

INITIAL ANGLE BETWEEN THE TORSO  
AND A VERTICAL LINE:

— 67.5°

- - - 45°

- + - 22.5°

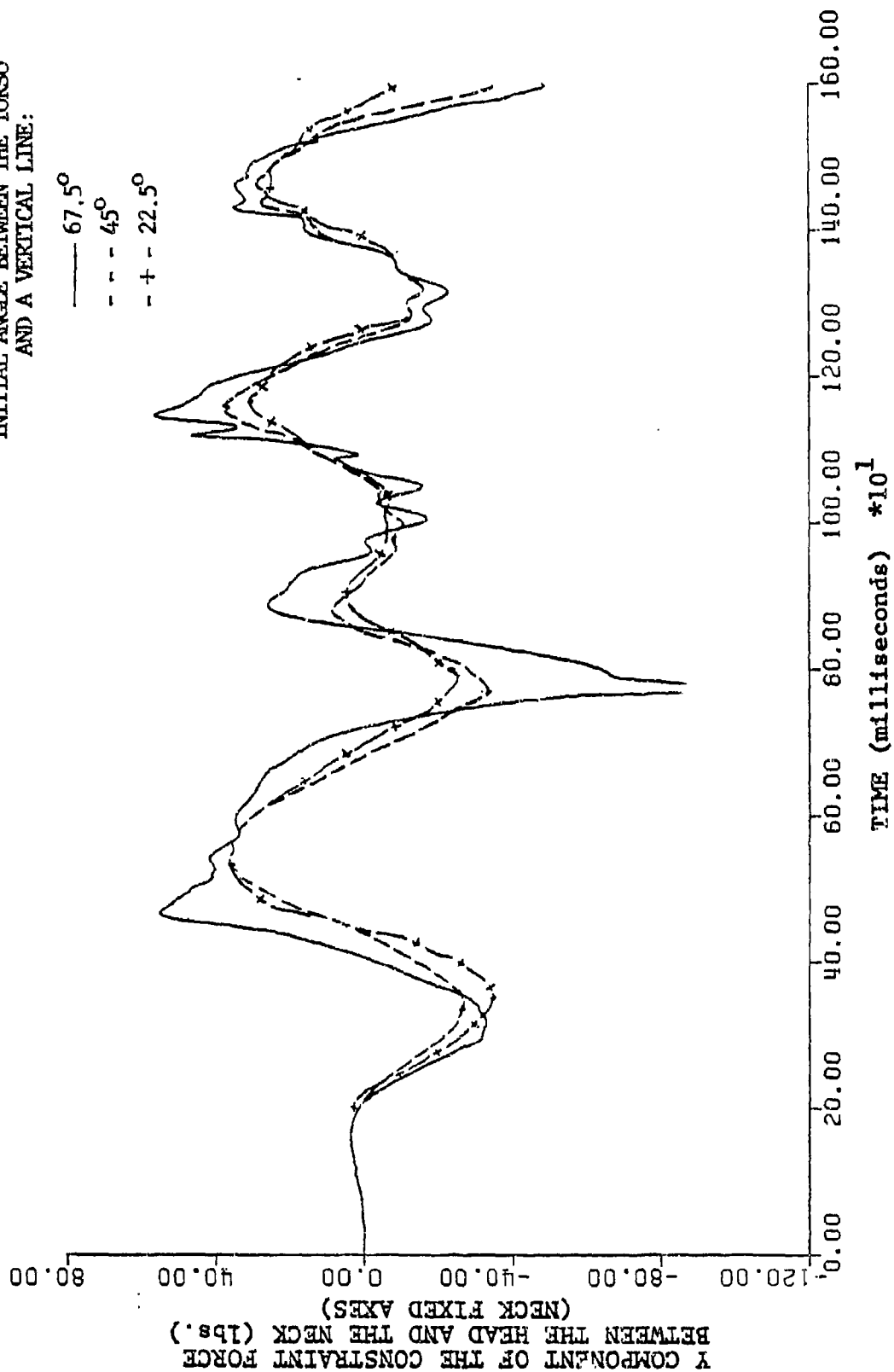


Figure 23. Y Component of the Constraint Force Between the Head and the Neck

Z COMPONENT OF THE CONSTRAINT FORCE  
BETWEEN THE HEAD AND THE NECK

INITIAL HEAD AND NECK ANGLES:  $0^{\circ}$

INITIAL ANGLE BETWEEN THE TORSO  
AND A VERTICAL LINE:

— 67.5°  
- - - 45°  
- + - 22.5°

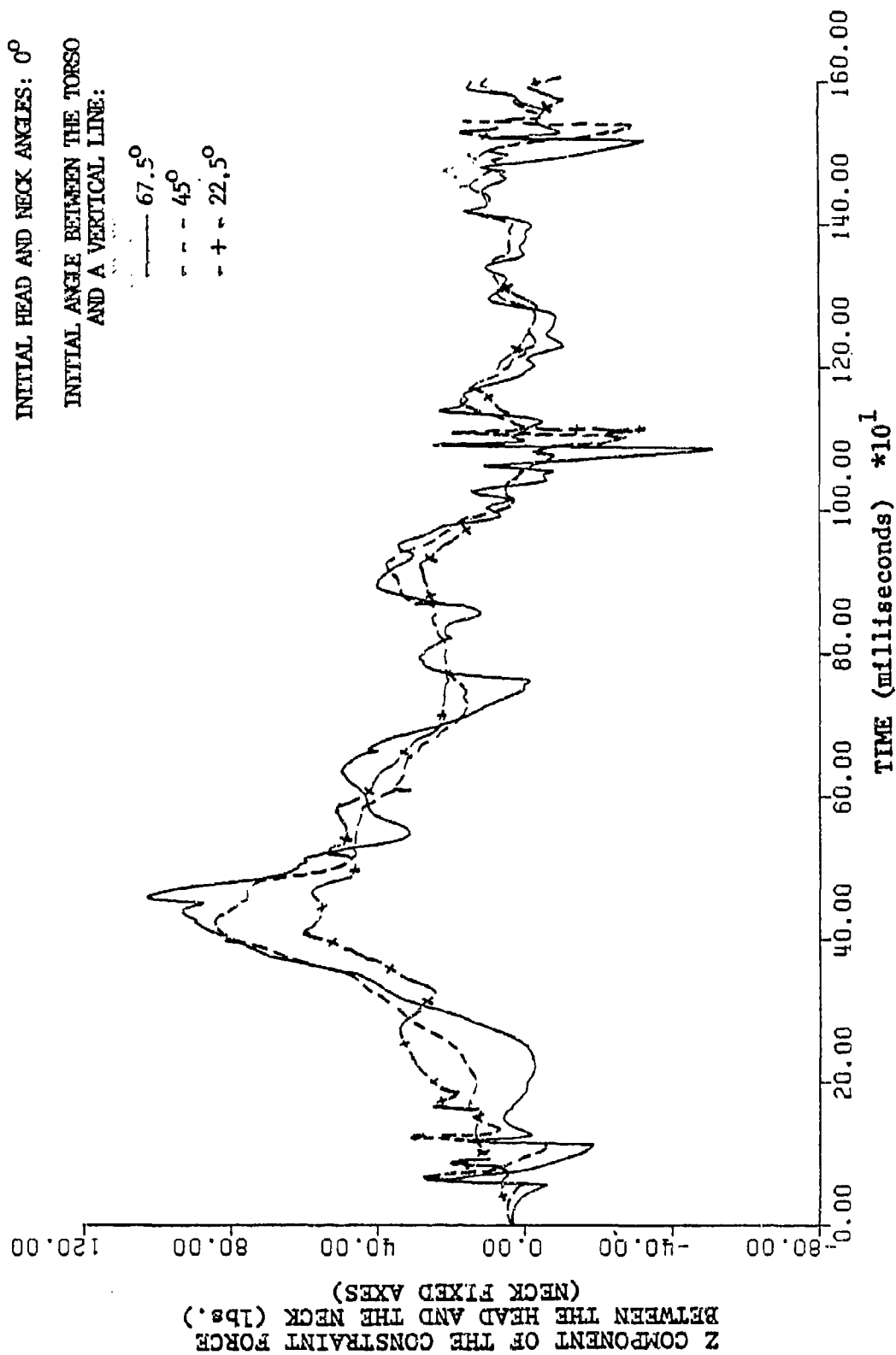


Figure 24. Z Component of the Constraint Force Between the Head and Neck

MAGNITUDE OF THE CONSTRAINT FORCE BETWEEN  
THE HEAD AND THE NECK

INITIAL HEAD AND NECK ANGLES:  $0^{\circ}$

INITIAL ANGLE BETWEEN THE TORSO  
AND A VERTICAL LINE:

—  $67.5^{\circ}$   
- - -  $45^{\circ}$   
- + -  $22.5^{\circ}$

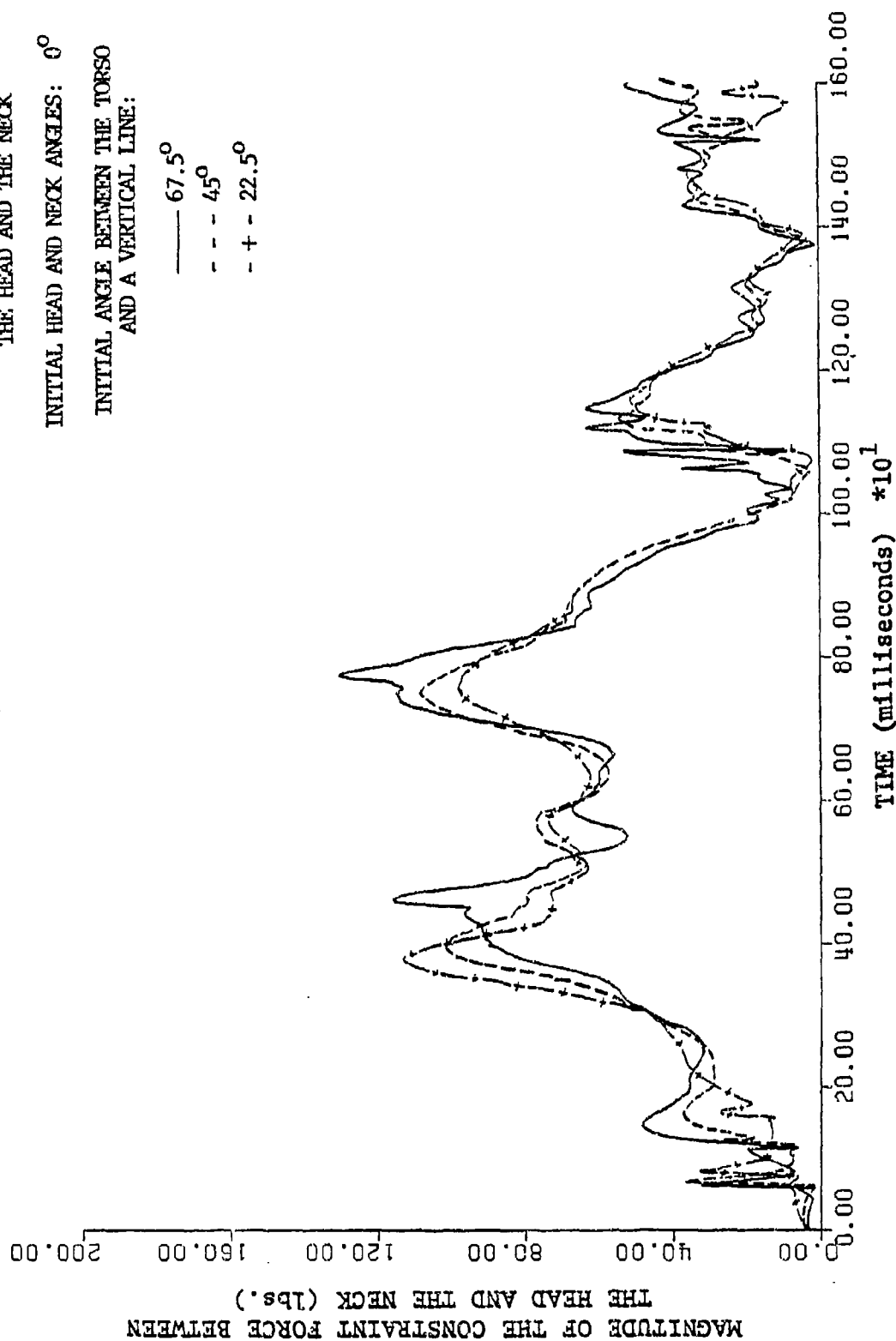


Figure 25. Magnitude of the Constraint Force Between the Head and the Neck

X COMPONENT OF THE CONSTRAINT FORCE BETWEEN  
THE HEAD AND THE NECK

INITIAL HEAD AND NECK ANGLES:  $15^{\circ}$

INITIAL ANGLE BETWEEN THE TORSO  
AND A VERTICAL LINE:

— 67.5°  
- - - 45°  
- + - 22.5°

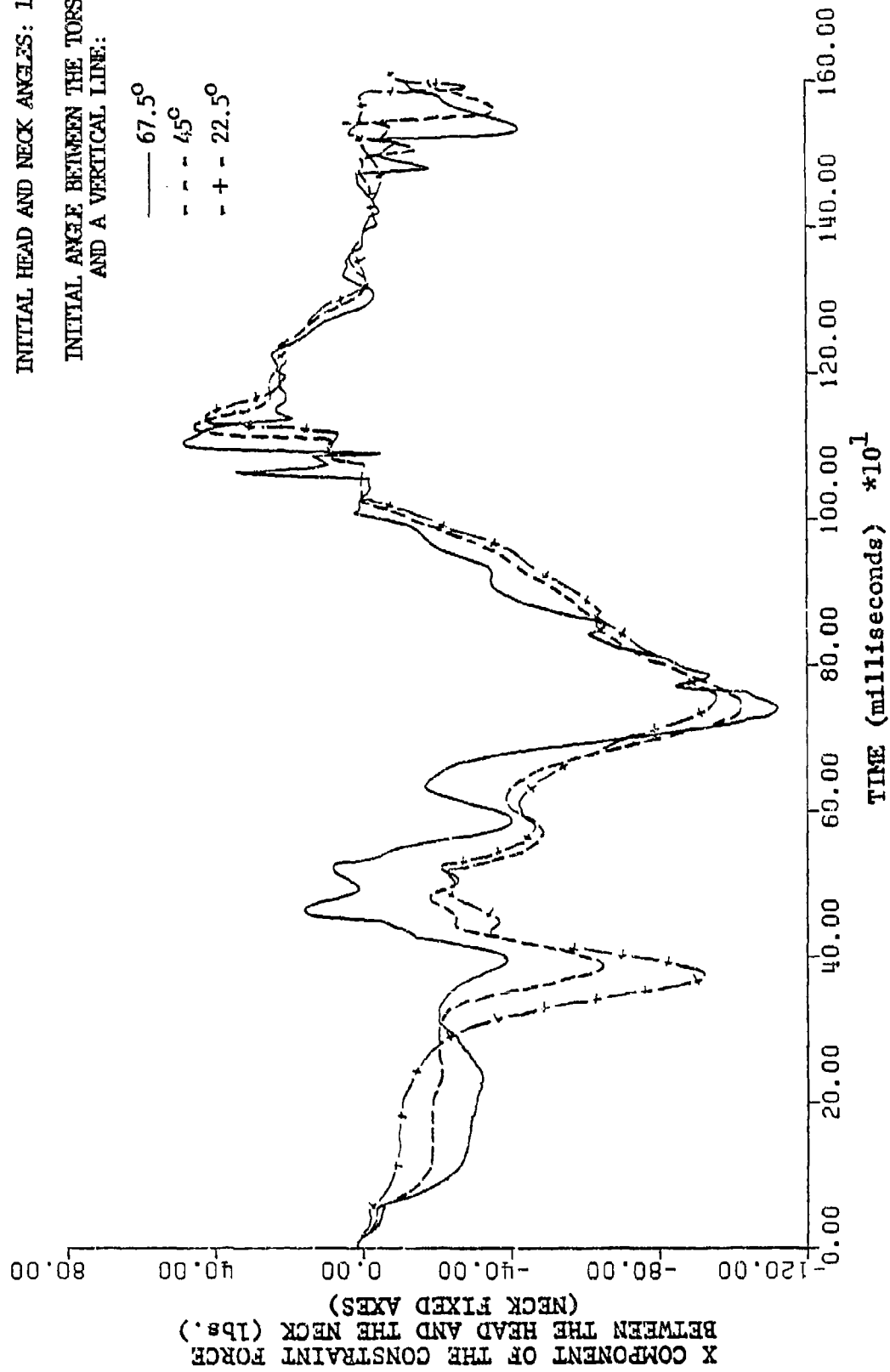


Figure 26. X Component of the Constraint Force Between the Head and the Neck



Y COMPONENT OF THE CONSTRAINT FORCE BETWEEN  
THE HEAD AND THE NECK

INITIAL HEAD AND NECK ANGLES:  $15^\circ$

INITIAL ANGLE BETWEEN THE TORSO  
AND A VERTICAL LINE:

—  $67.5^\circ$   
- - -  $45^\circ$   
- + -  $22.5^\circ$

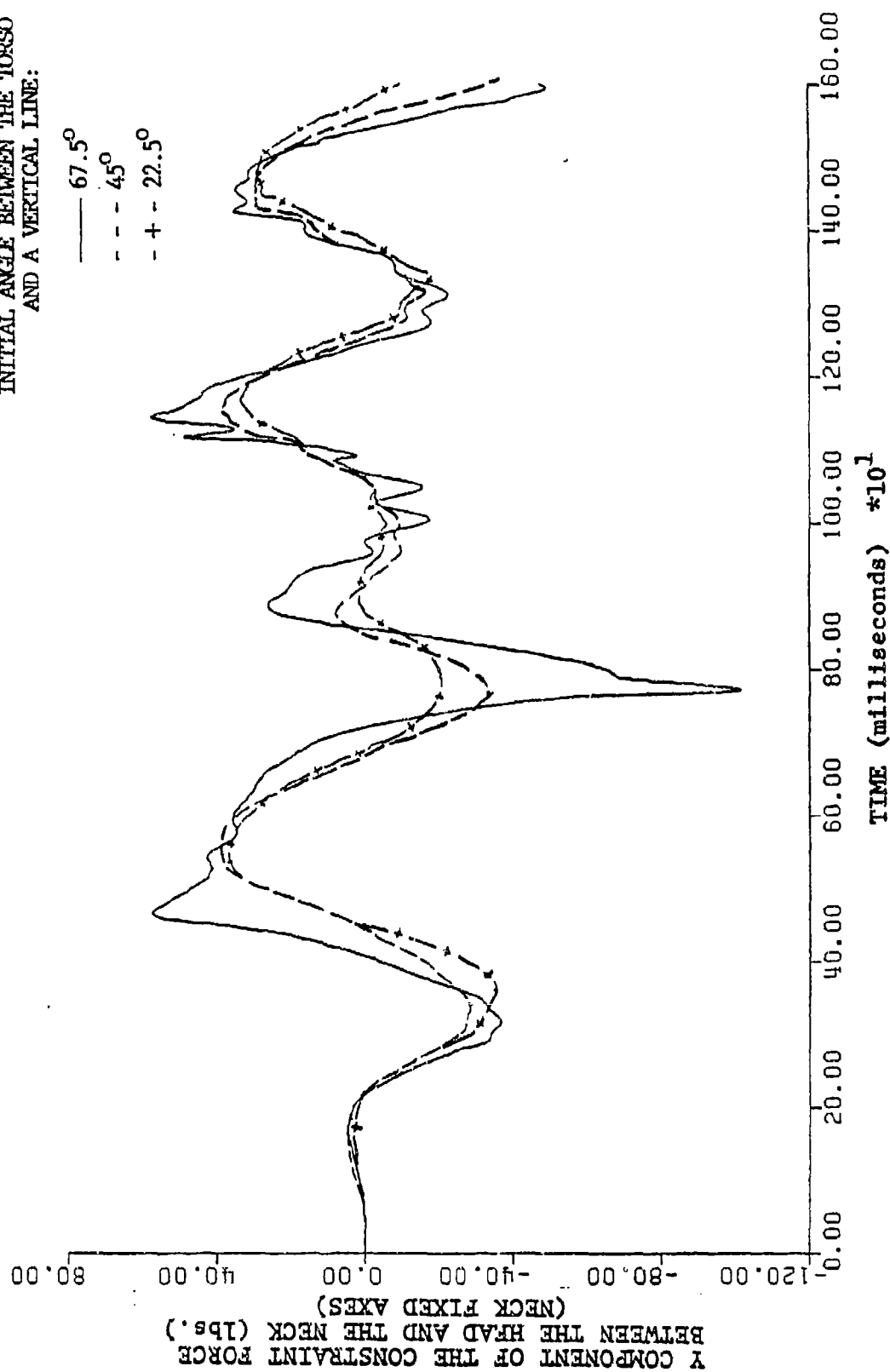


Figure 27. Y Component of the Constraint Force Between the Head and the Neck

Z COMPONENT OF THE CONSTRAINT FORCE BETWEEN  
THE HEAD AND THE NECK

INITIAL HEAD AND NECK ANGLES:  $15^{\circ}$

INITIAL ANGLE BETWEEN THE TORSO  
AND A VERTICAL LINE:

— 67.5°  
- - - 45°  
- + - 22.5°

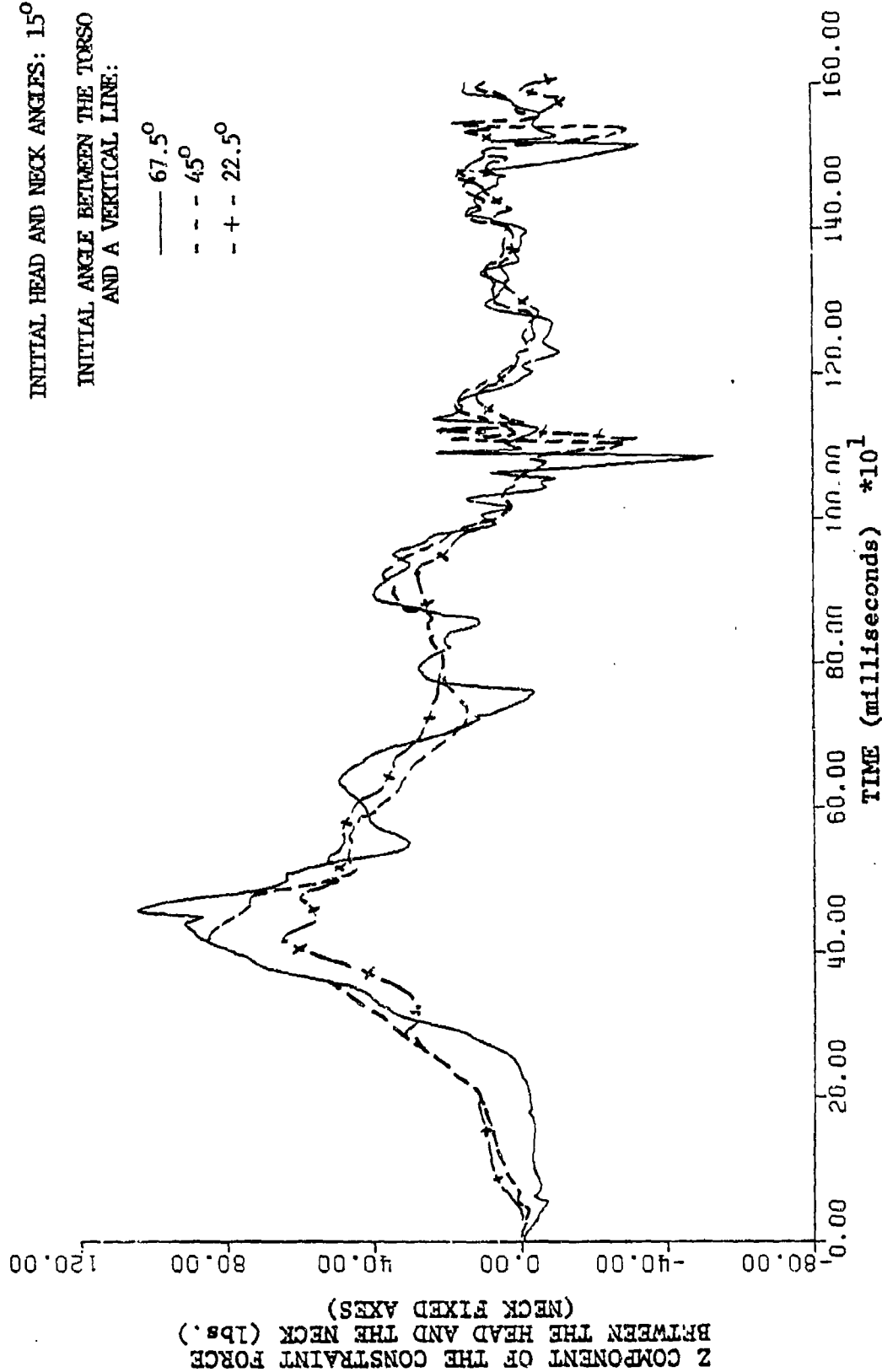


Figure 28. Z Component of the Constraint Force Between the Head and the Neck

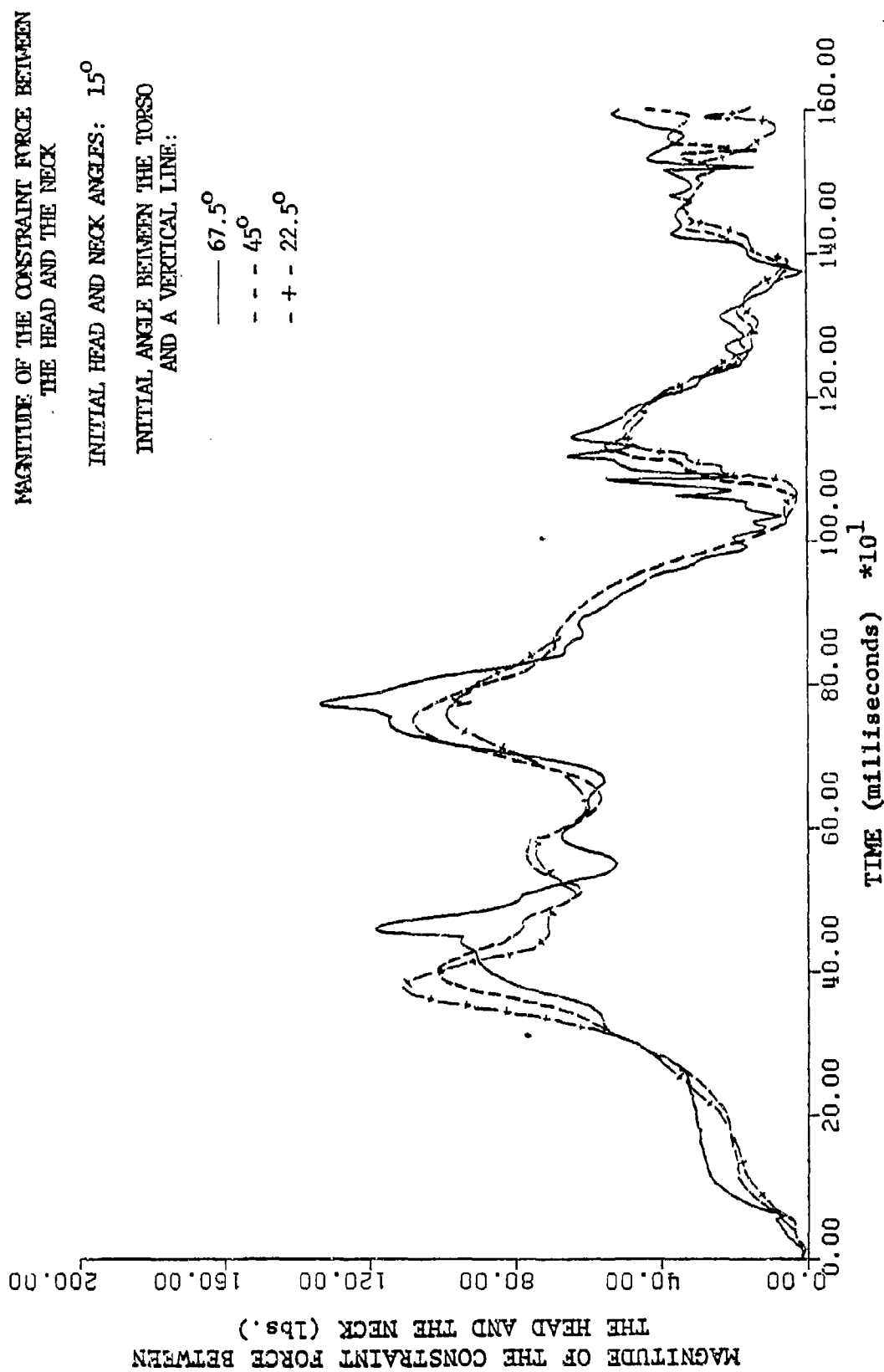


Figure 29. Magnitude of the Constraint Force Between the Head and the Neck

X COMPONENT OF THE TORQUE APPLIED BETWEEN  
THE HEAD AND THE NECK

INITIAL HEAD AND NECK ANGLES:  $-15^{\circ}$

INITIAL ANGLE BETWEEN THE TORSO  
AND A VERTICAL LINE:

—  $67.5^{\circ}$   
- - -  $45^{\circ}$   
- + -  $22.5^{\circ}$

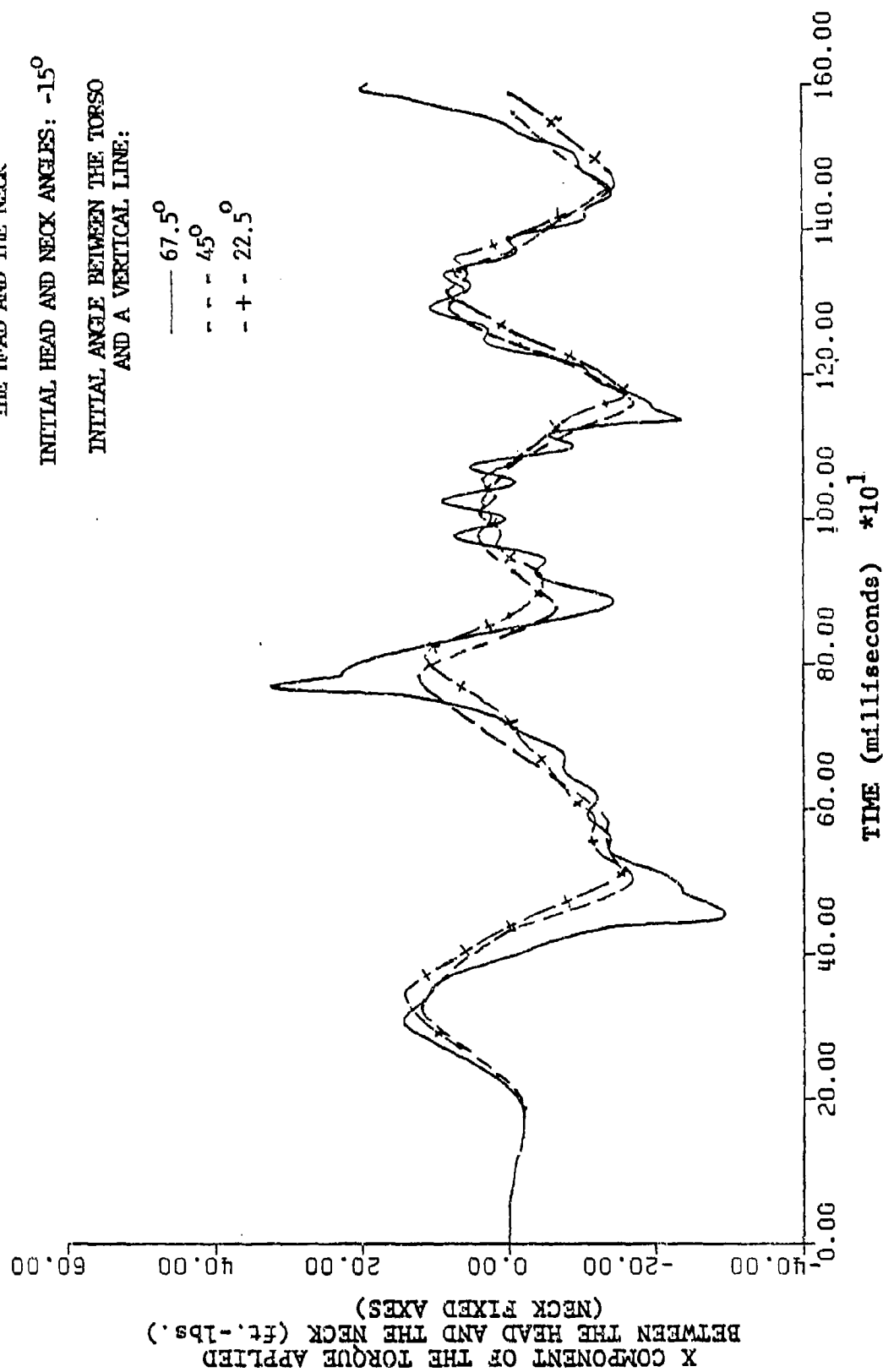


Figure 30. X Component of the Torque Applied Between the Head and the Neck

Y COMPONENT OF THE TORQUE APPLIED BETWEEN  
THE HEAD AND THE NECK

INITIAL HEAD AND NECK ANGLES:  $-15^{\circ}$

INITIAL ANGLE BETWEEN THE TORSO  
AND A VERTICAL LINE:

— 67.5°  
- - - 45°  
- + - 22.5°

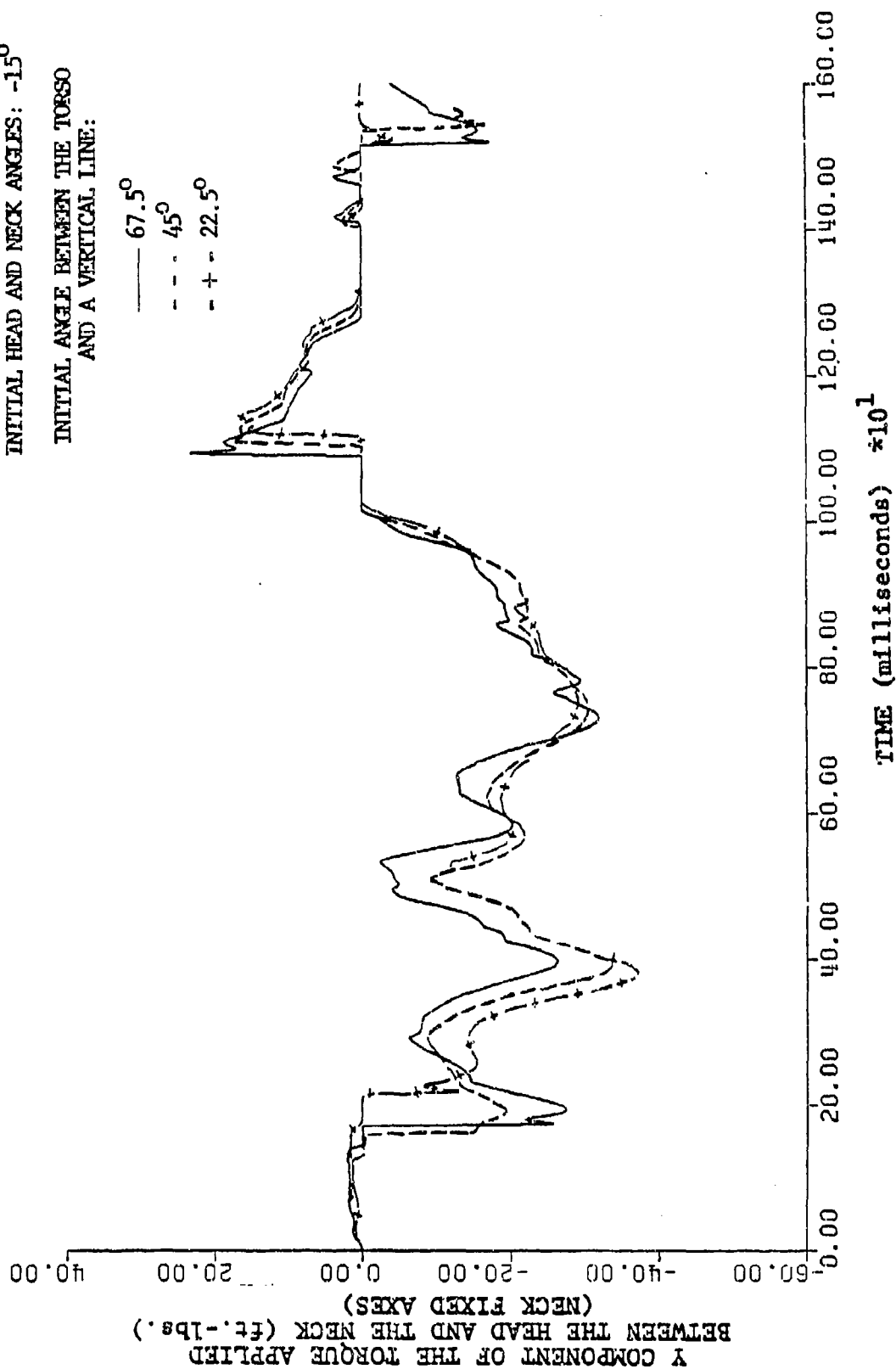


Figure 31. Y Component of the Torque Applied Between the Head and the Neck

MAGNITUDE OF THE TORQUE APPLIED BETWEEN  
THE HEAD AND THE NECK

INITIAL HEAD AND NECK ANGLES:  $-15^{\circ}$

INITIAL ANGLE BETWEEN THE TORSO  
AND A VERTICAL LINE:

—  $67.5^{\circ}$   
- - -  $45^{\circ}$   
- + -  $22.5^{\circ}$

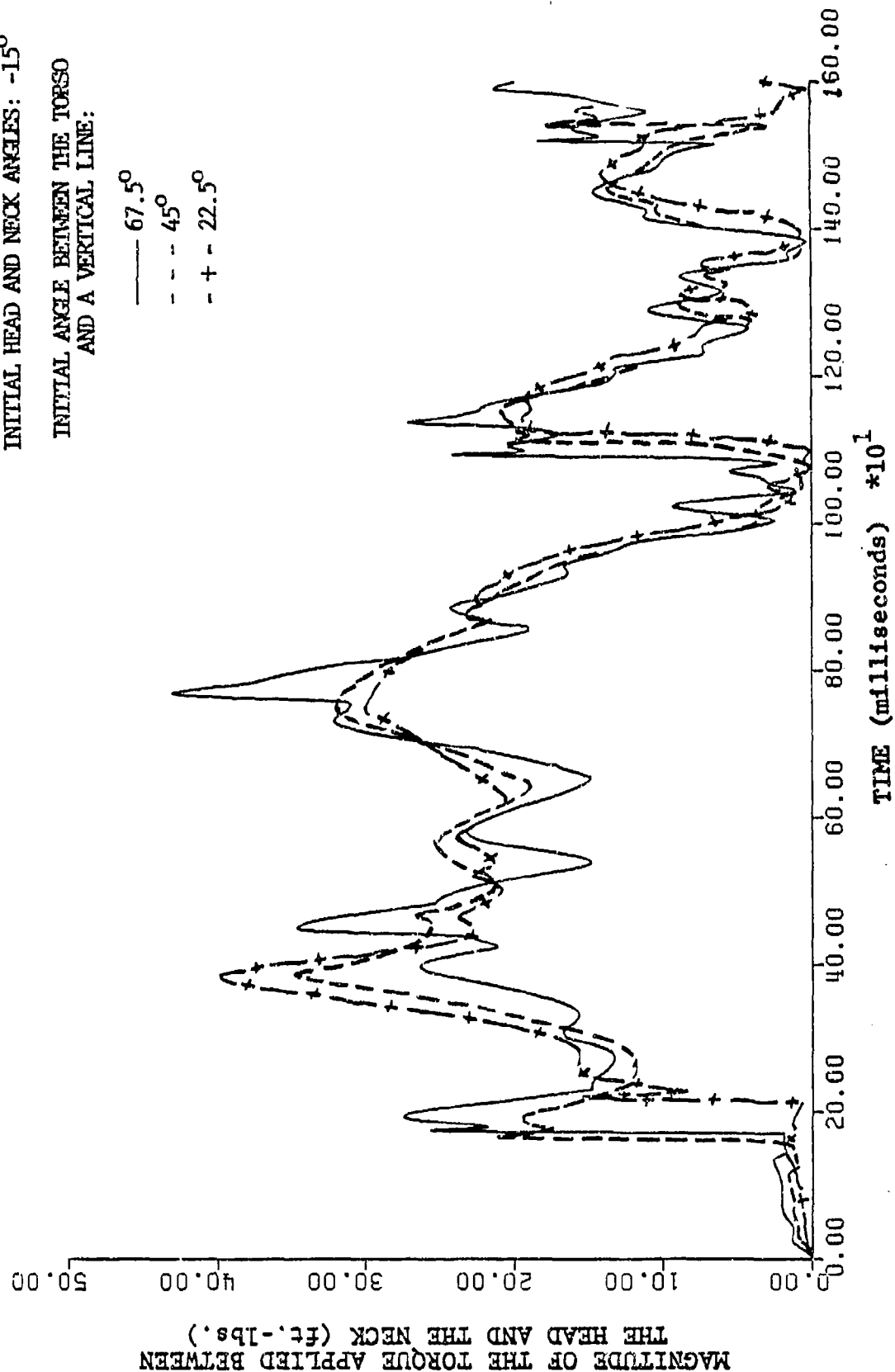


Figure 32. Magnitude of the Torque Applied Between the Head and the Neck

X COMPONENT OF THE TORQUE APPLIED BETWEEN  
THE HEAD AND THE NECK

INITIAL HEAD AND NECK ANGLES:  $0^{\circ}$   
INITIAL ANGLE BETWEEN THE TORSO  
AND A VERTICAL LINE:

—  $67.5^{\circ}$   
- - -  $45^{\circ}$   
- + -  $22.5^{\circ}$

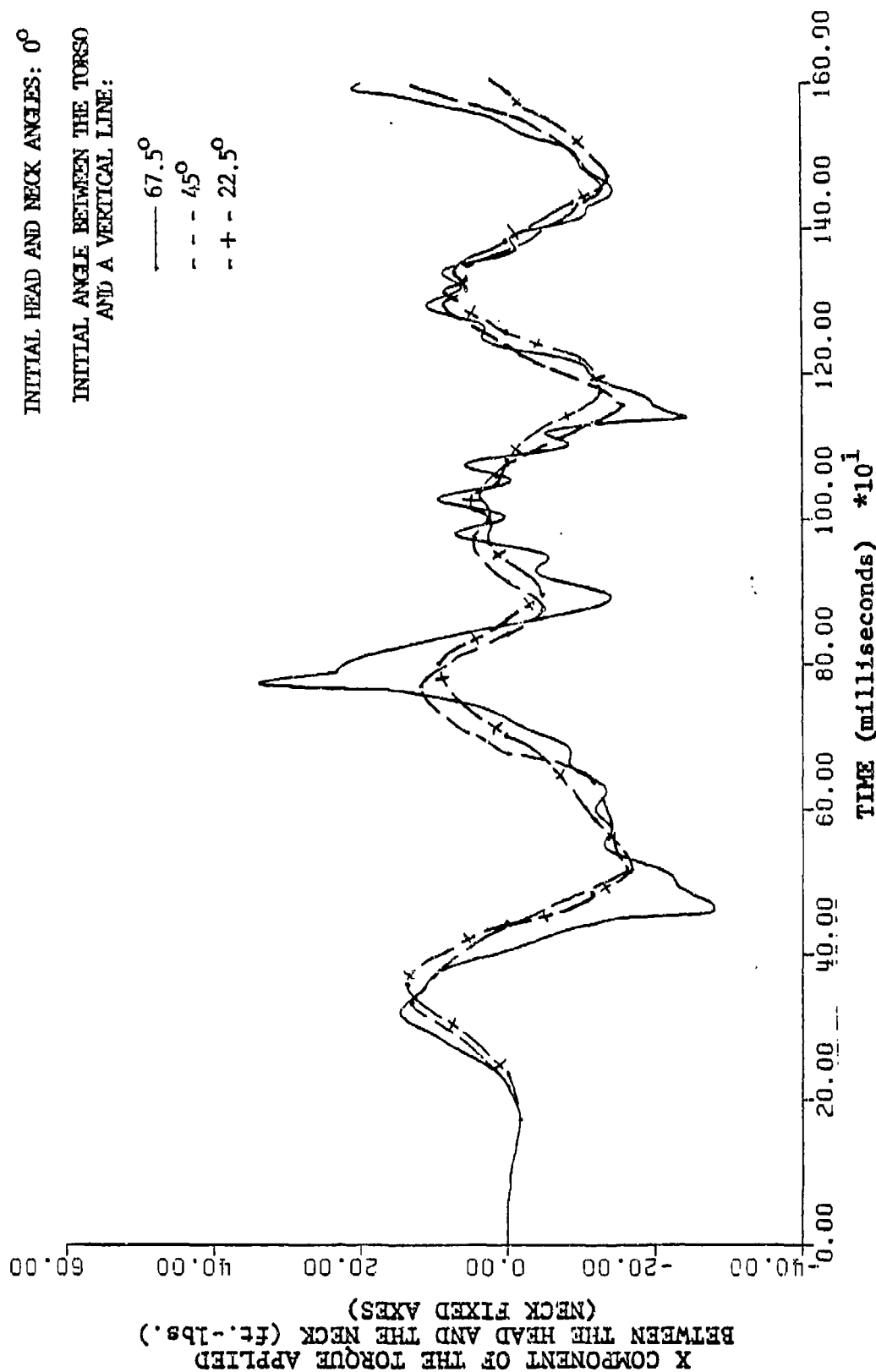


Figure 33. X Component of the Torque Applied Between the Head and the Neck

Y COMPONENT OF THE TORQUE APPLIED BETWEEN  
THE HEAD AND THE NECK

INITIAL HEAD AND NECK ANGLES:  $0^{\circ}$

INITIAL ANGLE BETWEEN THE TORSO  
AND A VERTICAL LINE:

— 67.5°  
- - - 45°  
- + - 22.5°

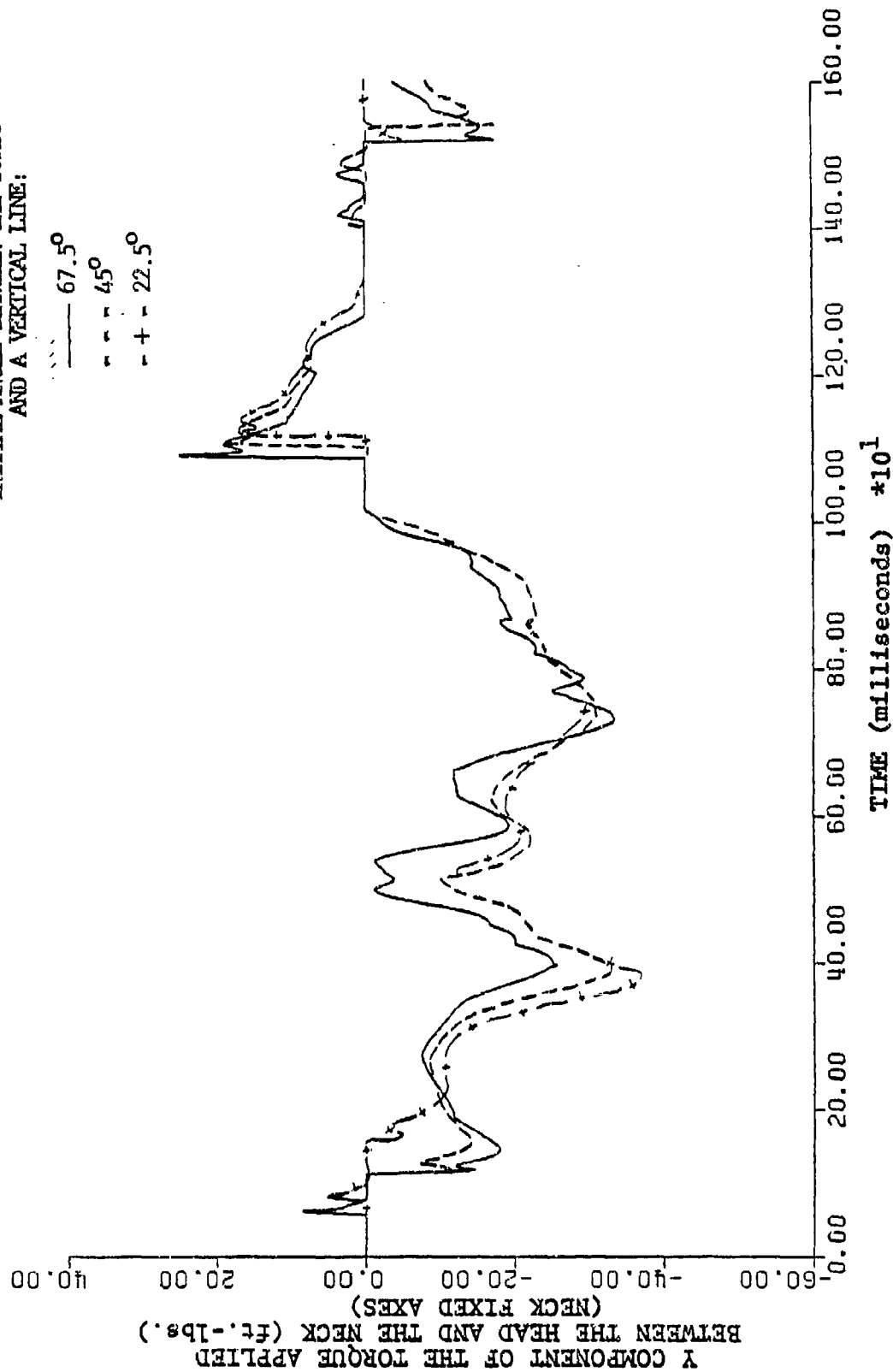


Figure 34. Y Component of the Torque Applied Between the Head and the Neck



MAGNITUDE OF THE TORQUE APPLIED BETWEEN  
THE HEAD AND THE NECK

INITIAL HEAD AND NECK ANGLES:  $0^{\circ}$

INITIAL ANGLE BETWEEN THE TORSO  
AND A VERTICAL LINE:

—  $67.5^{\circ}$   
- - -  $45^{\circ}$   
- + -  $22.5^{\circ}$

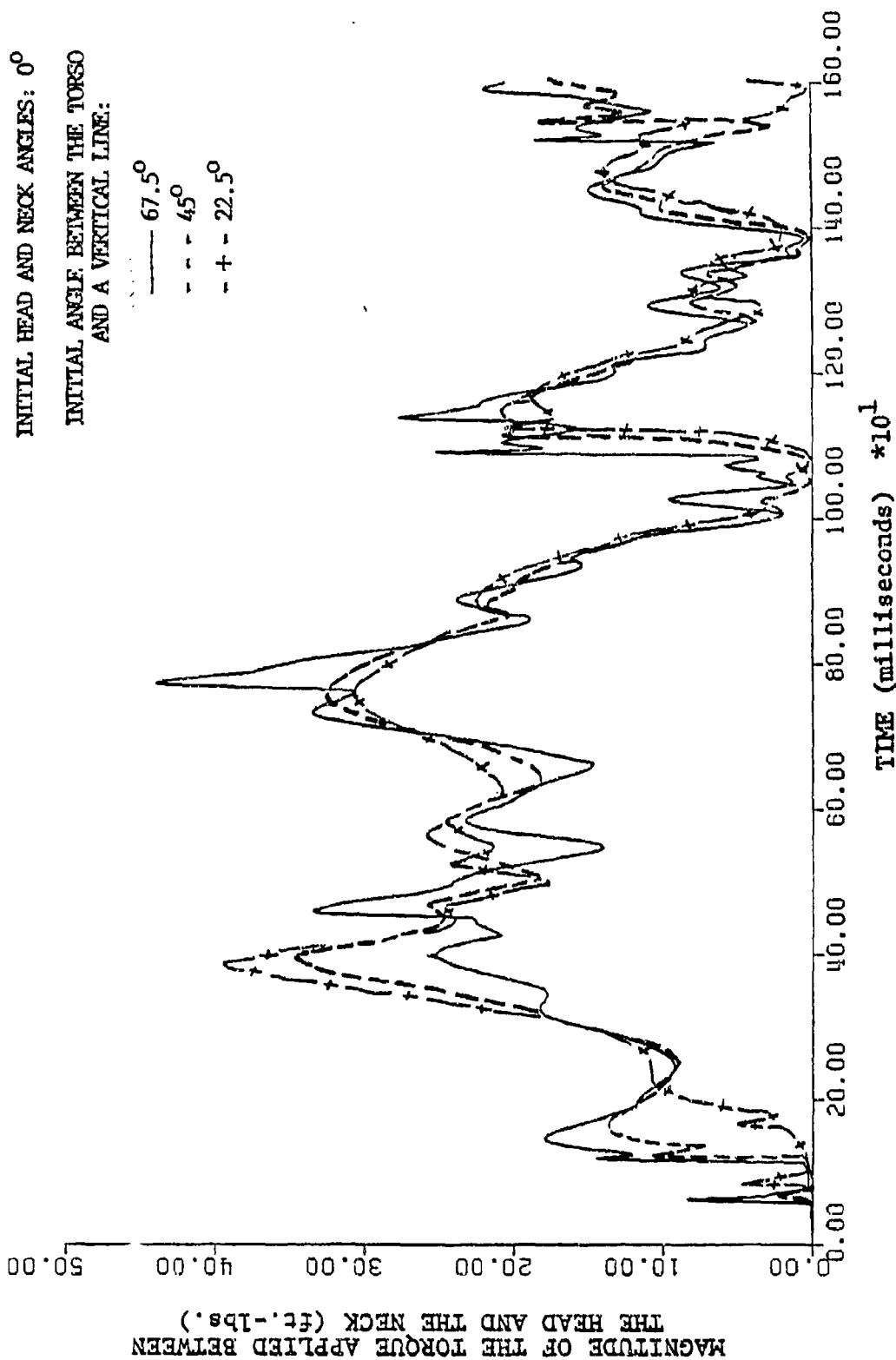


Figure 35, Magnitude of the Torque Applied Between the Head and the Neck

X COMPONENT OF THE TORQUE APPLIED BETWEEN  
THE HEAD AND THE NECK

INITIAL HEAD AND NECK ANGLES:  $15^\circ$

INITIAL ANGLE BETWEEN THE TORSO  
AND A VERTICAL LINE

—  $67.5^\circ$   
- - -  $45^\circ$   
- + -  $22.5^\circ$

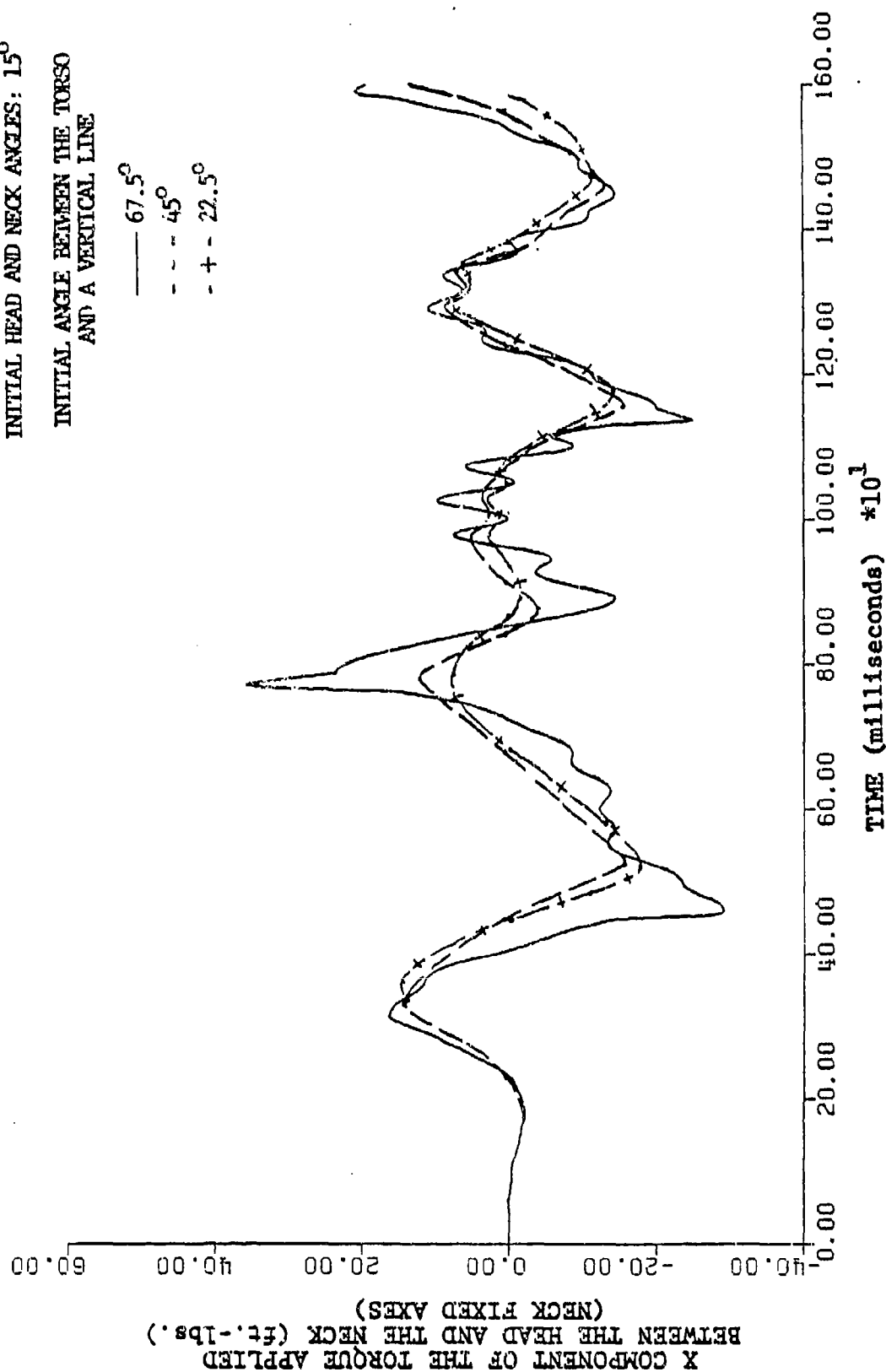


Figure 36. X Component of the Torque Applied Between the Head and the Neck

Y COMPONENT OF THE TORQUE APPLIED BETWEEN  
THE HEAD AND THE NECK

INITIAL HEAD AND NECK ANGLES:  $15^{\circ}$

INITIAL ANGLE BETWEEN THE TORSO  
AND A VERTICAL LINE:

—  $67.5^{\circ}$   
- - -  $45^{\circ}$   
- + -  $22.5^{\circ}$

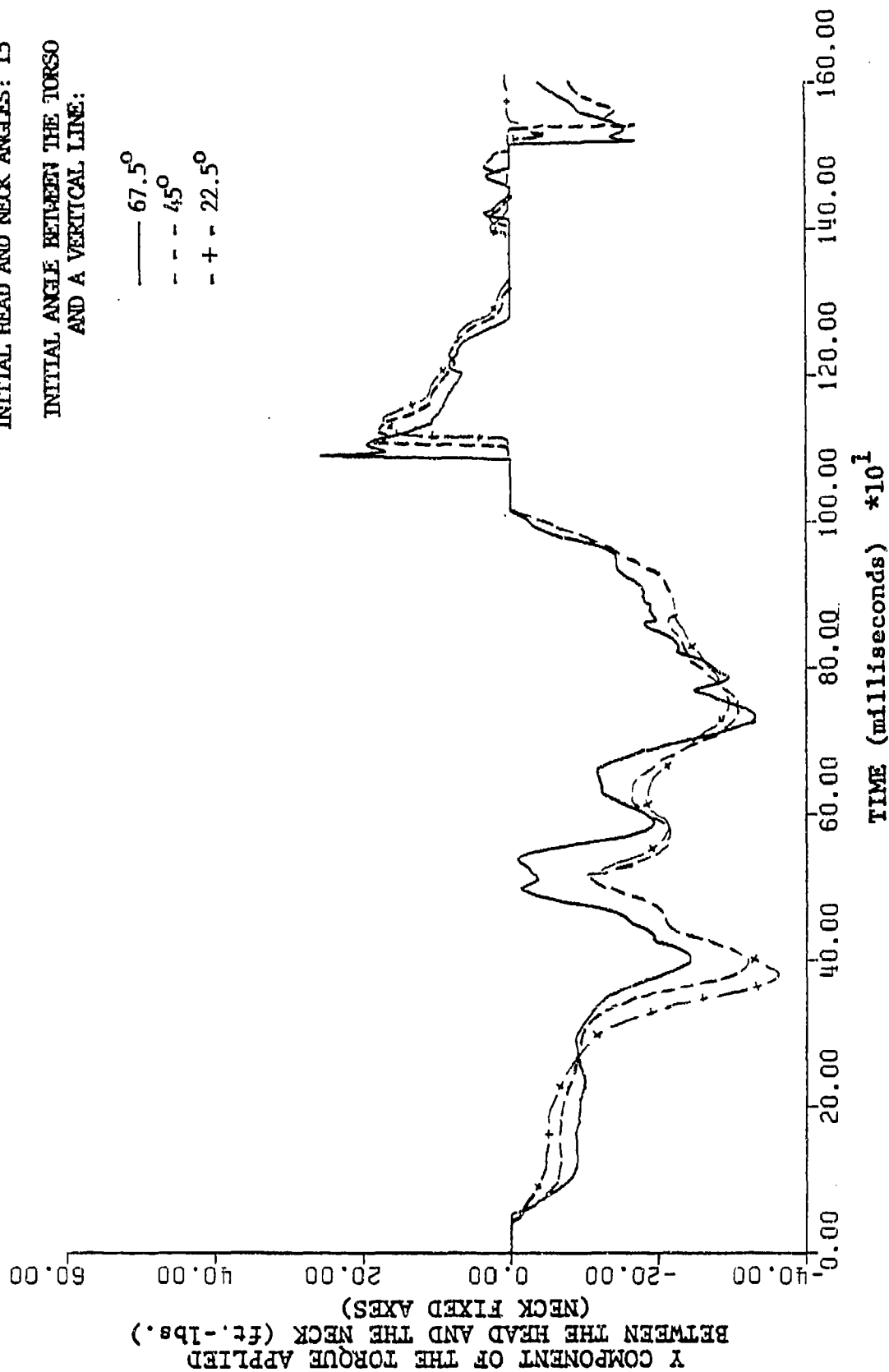


Figure 37. Y Component of the Torque Applied Between the Head and the Neck

MAGNITUDE OF THE TORQUE APPLIED BETWEEN  
THE HEAD AND THE NECK

INITIAL HEAD AND NECK ANGLES:  $15^{\circ}$

INITIAL ANGLE BETWEEN THE TORSO  
AND A VERTICAL LINE:

—  $67.5^{\circ}$   
- - -  $45^{\circ}$   
- + -  $22.5^{\circ}$

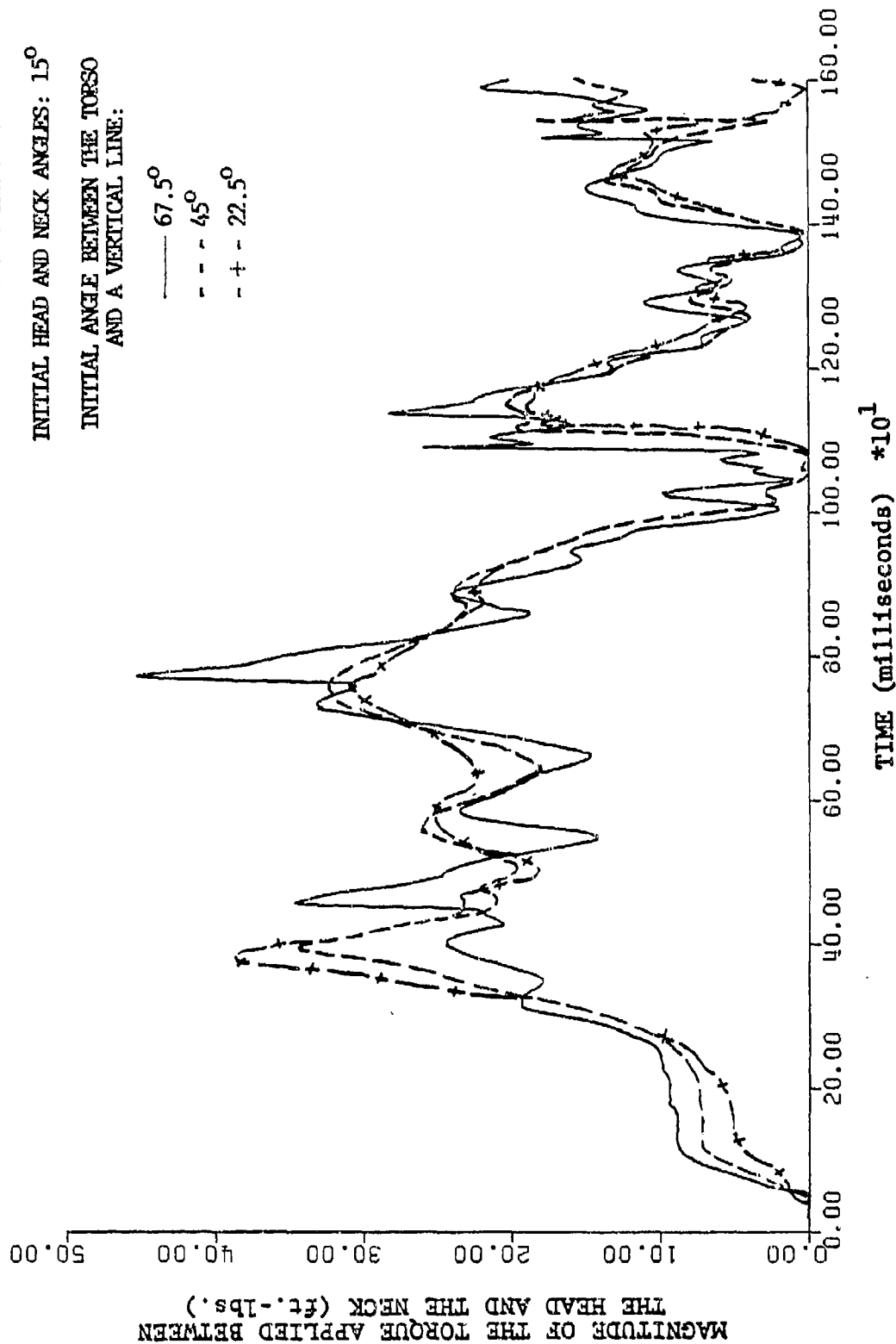


Figure 38. Magnitude of the Torque Applied Between the Head and the Neck

Y COMPONENT OF THE ANGULAR ACCELERATION OF THE  
HEAD RELATIVE TO THE TORSO

INITIAL HEAD AND NECK ANGLES:  $-15^{\circ}$

INITIAL ANGLE BETWEEN THE TORSO  
AND A VERTICAL LINE:

—  $67.5^{\circ}$   
- - -  $45^{\circ}$   
- + -  $22.5^{\circ}$

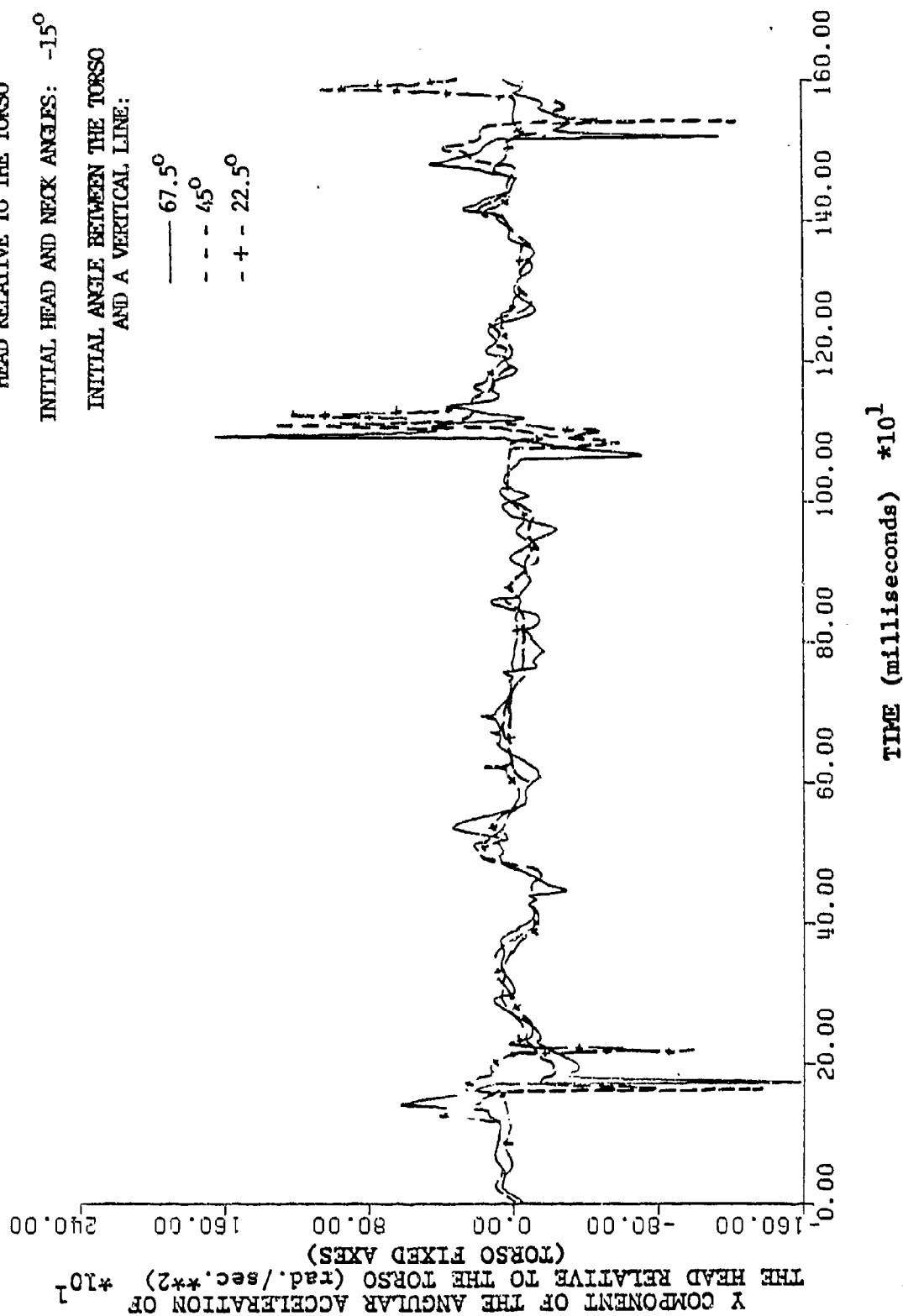


Figure 39. Y Component of the Angular Acceleration of the Head Relative to the Torso

Y COMPONENT OF THE ANGULAR ACCELERATION OF  
THE HEAD RELATIVE TO THE TORSO

INITIAL HEAD AND NECK ANGLES:  $0^{\circ}$

INITIAL ANGLE BETWEEN THE TORSO  
AND A VERTICAL LINE:

— 67.5°  
- - - 45°  
+ - 22.5°

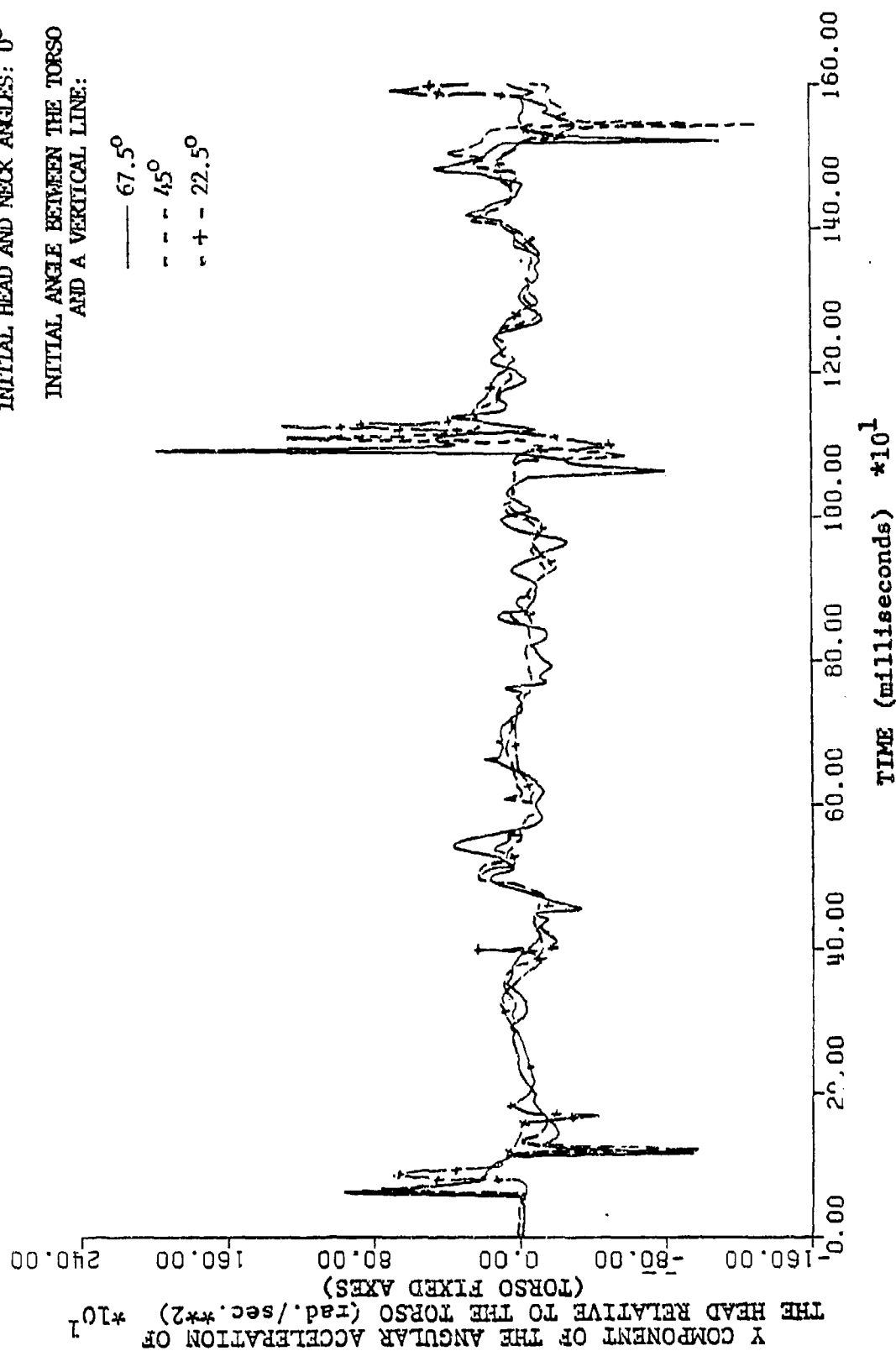


Figure 40. Y Component of the Angular Acceleration of the Head Relative to the Torso

Y COMPONENT OF THE ANGULAR ACCELERATION OF THE  
HEAD RELATIVE TO THE TORSO

INITIAL HEAD AND NECK ANGLES:  $15^{\circ}$

INITIAL ANGLE BETWEEN THE TORSO  
AND A VERTICAL LINE:

—  $67.5^{\circ}$   
- - -  $45^{\circ}$   
- + -  $22.5^{\circ}$

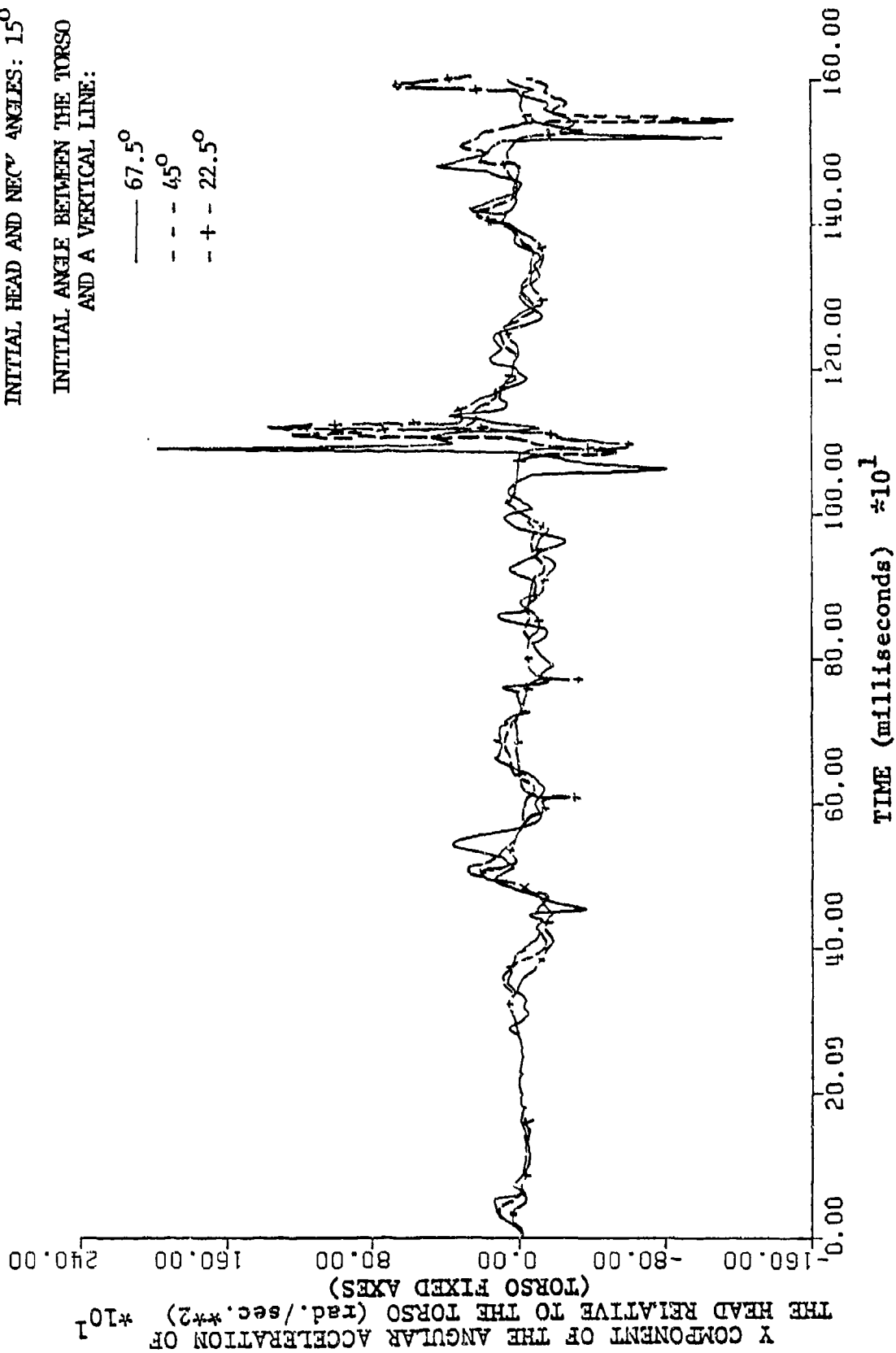


Figure 41. Y Component of the Angular Acceleration of the Head Relative to the Torso

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